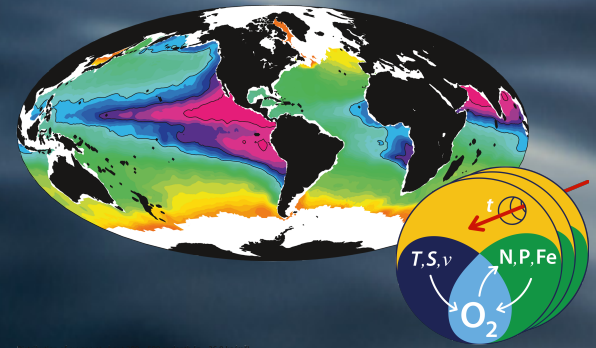


PIRATA 23, Marseilles
October 23, 2018



Ventilation of the eastern tropical North Atlantic oxygen minimum zone by latitudinally alternating zonal jets in a shallow water model

SFB 754

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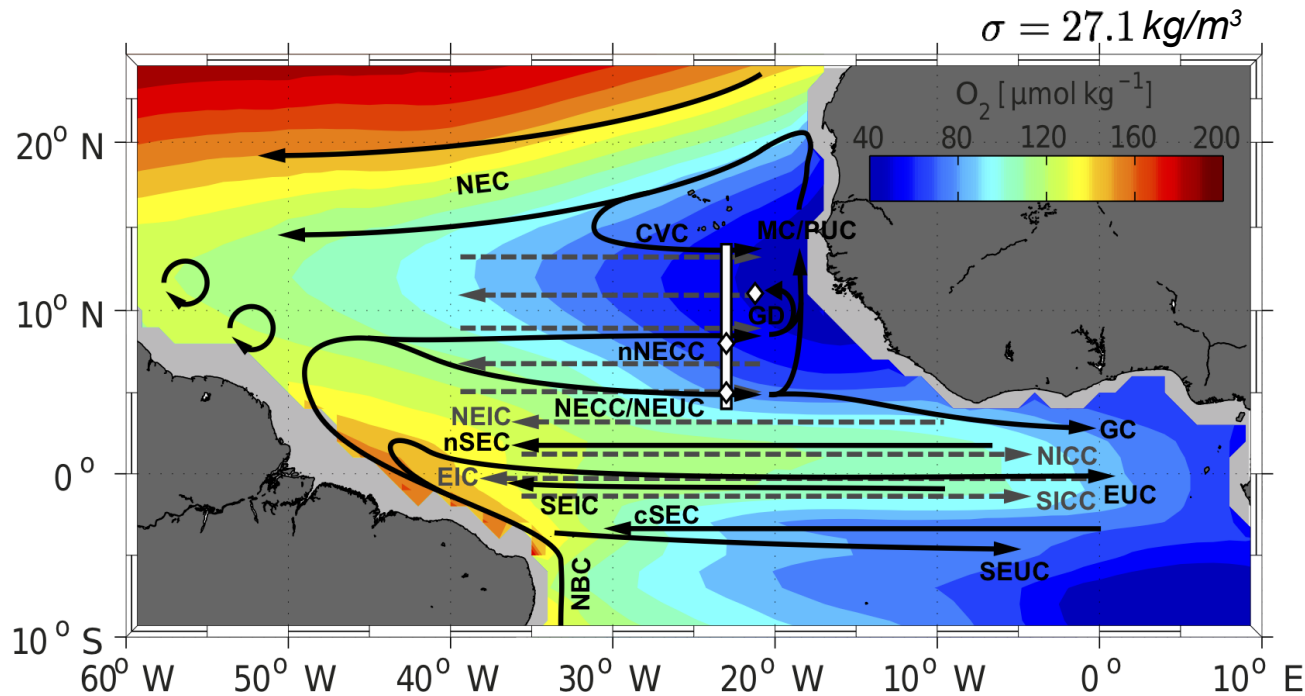
² Faculty of Mathematics and Natural Sciences, Christian-Albrechts-Universität zu Kiel, Germany

HELMHOLTZ

RESEARCH FOR GRAND CHALLENGES

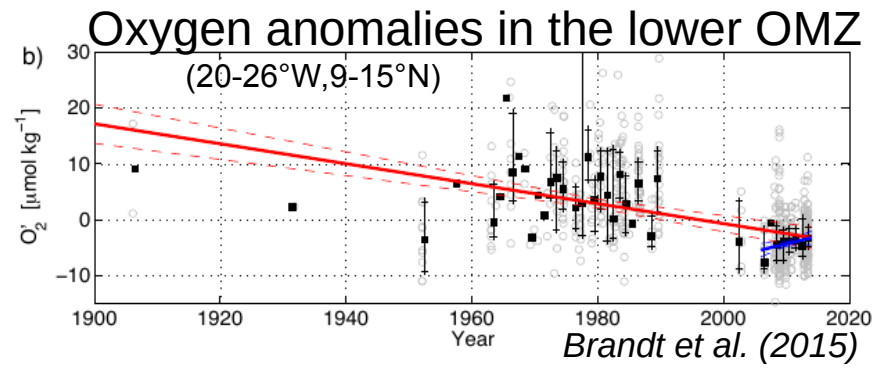
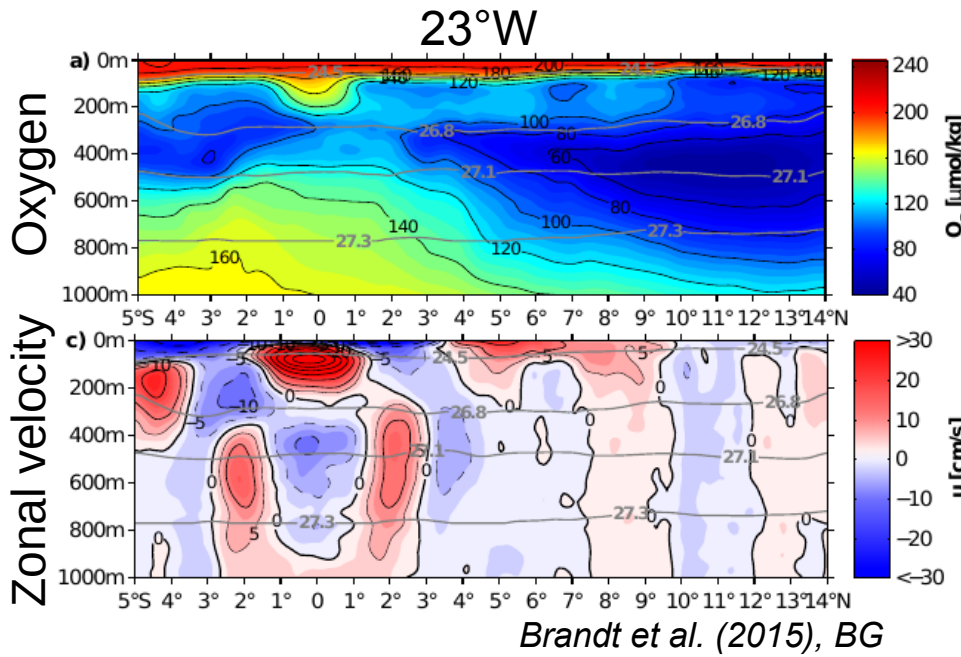
GEOMAR 

The oxygen minimum zone (OMZ) in the eastern tropical North Atlantic (ETNA)



Hahn et al. (2017), OS

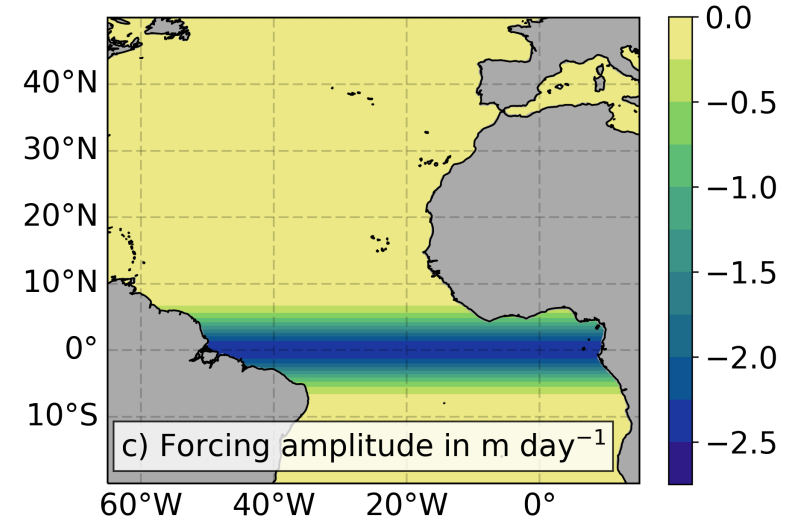
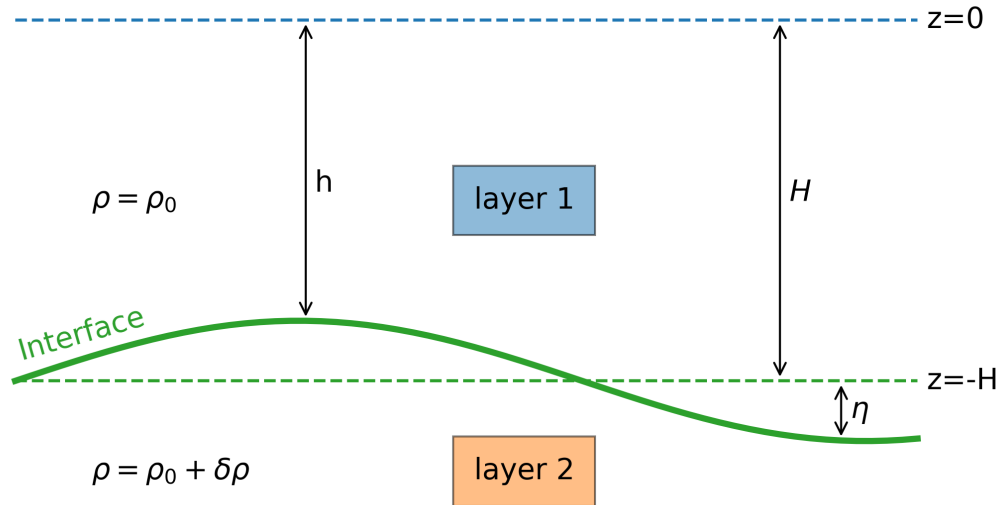
Ventilation of the ETNA OMZ by latitudinally alternating zonal jets (LAZJs)



➔ LAZJs are suspected to matter for long term variability of OMZ ventilation (Brandt et al. 2015, BG)

➔ turn to non-linear shallow water model to study the LAZJ variability and its effect on the ETNA OMZ ventilation

Non-linear shallow water model

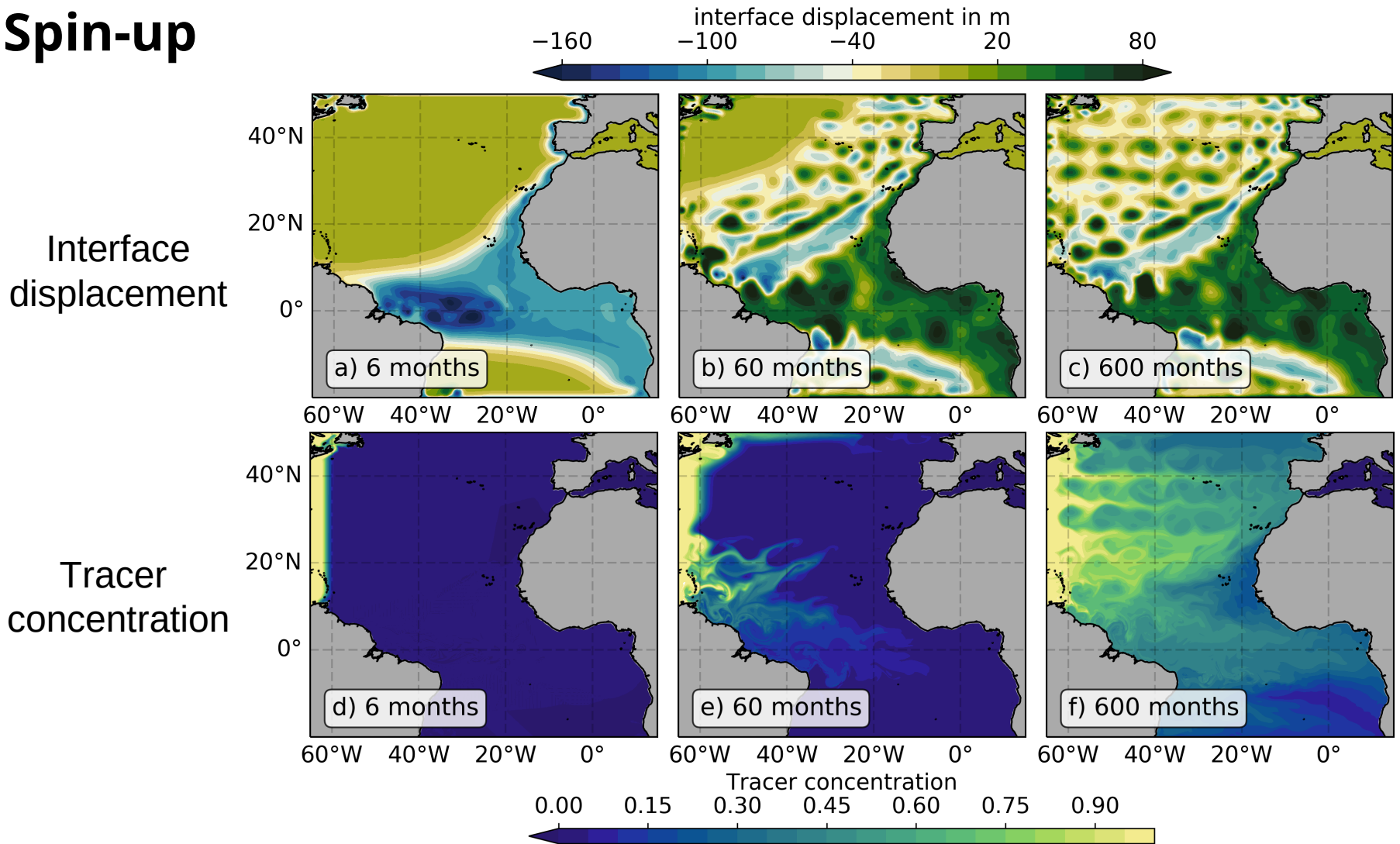


➔ coupled to an advection-diffusion model with tracer (C) set-up to mimic oxygen

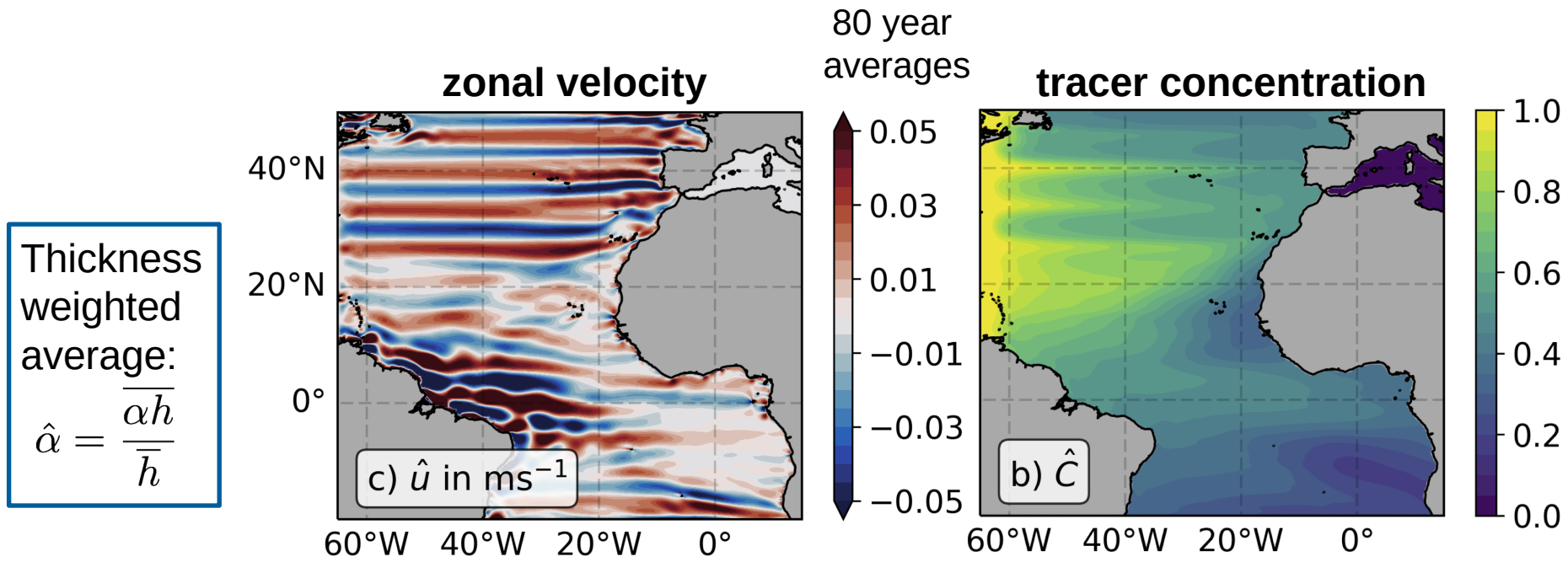
$$\underbrace{\frac{\partial(Ch)}{\partial t}}_1 + \underbrace{\nabla \cdot (Ch\mathbf{u})}_2 = \underbrace{\nabla \cdot (\kappa_h h \nabla C)}_3 - \underbrace{JCh}_4 - \underbrace{h\gamma(C - C_0)}_5 + \underbrace{CF_\eta}_6 \quad \begin{array}{l} \gamma \approx 1/8 \text{ day}^{-1} \\ J \approx 1/49 \text{ year}^{-1} \end{array}$$

- 1) tendency 2) advective terms 3) diffusion 4) consumption 5) source (western boundary) 6) forcing

Spin-up

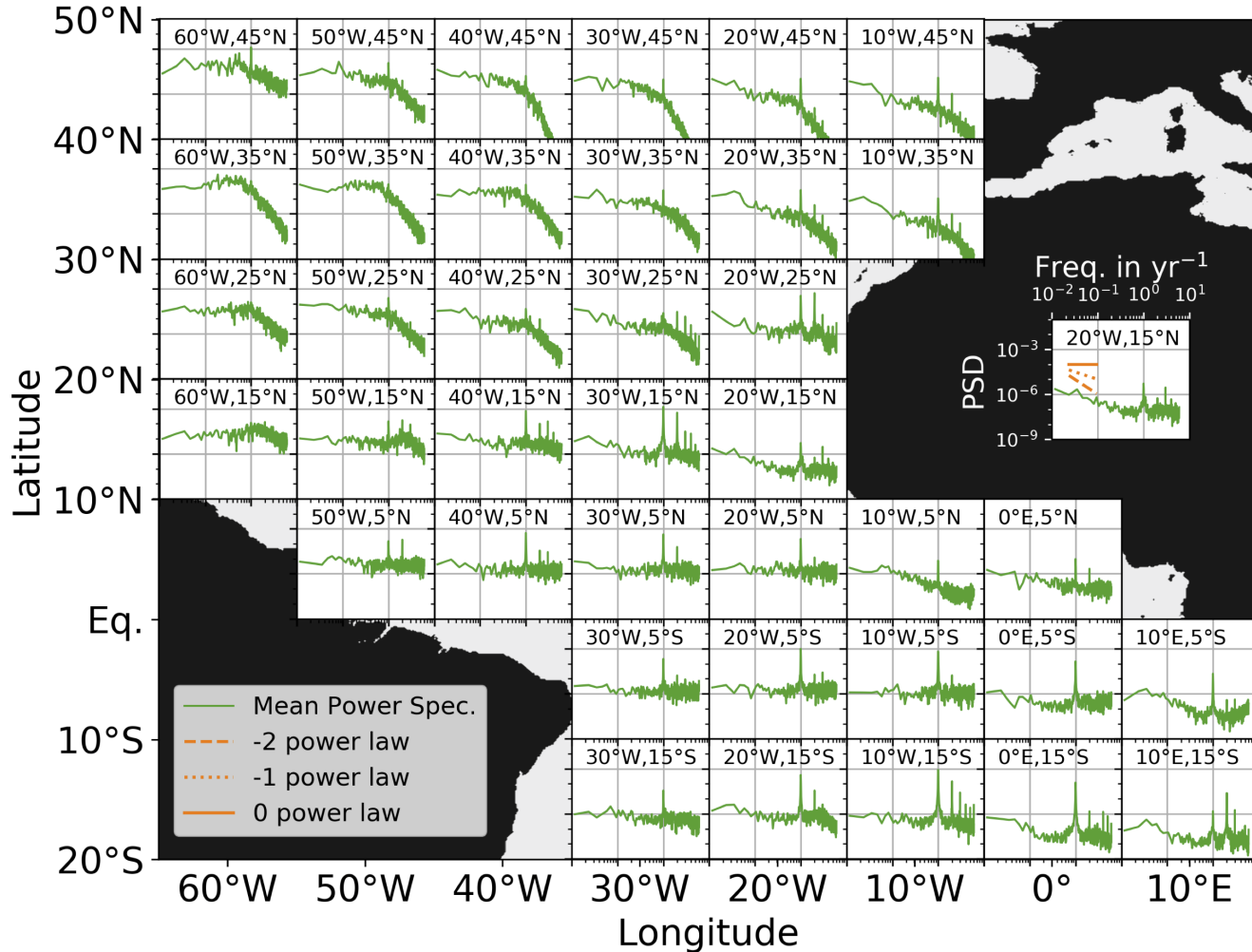


Statistical mean state features LAZJs and ETNA OMZ

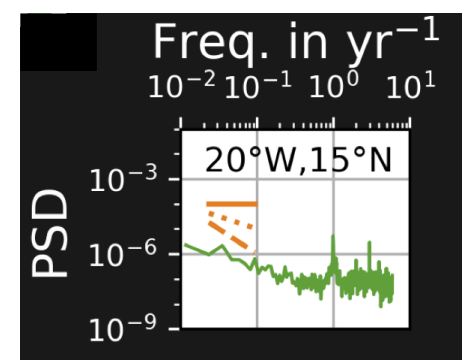


- ➔ meridional scale of LAZJs is wider than Rossby radius and Rhines scale
- ➔ LAZJs mainly driven by eddies whose size is set by non-linear triad instability process (cf. Qiu et al. 2013, JPO)

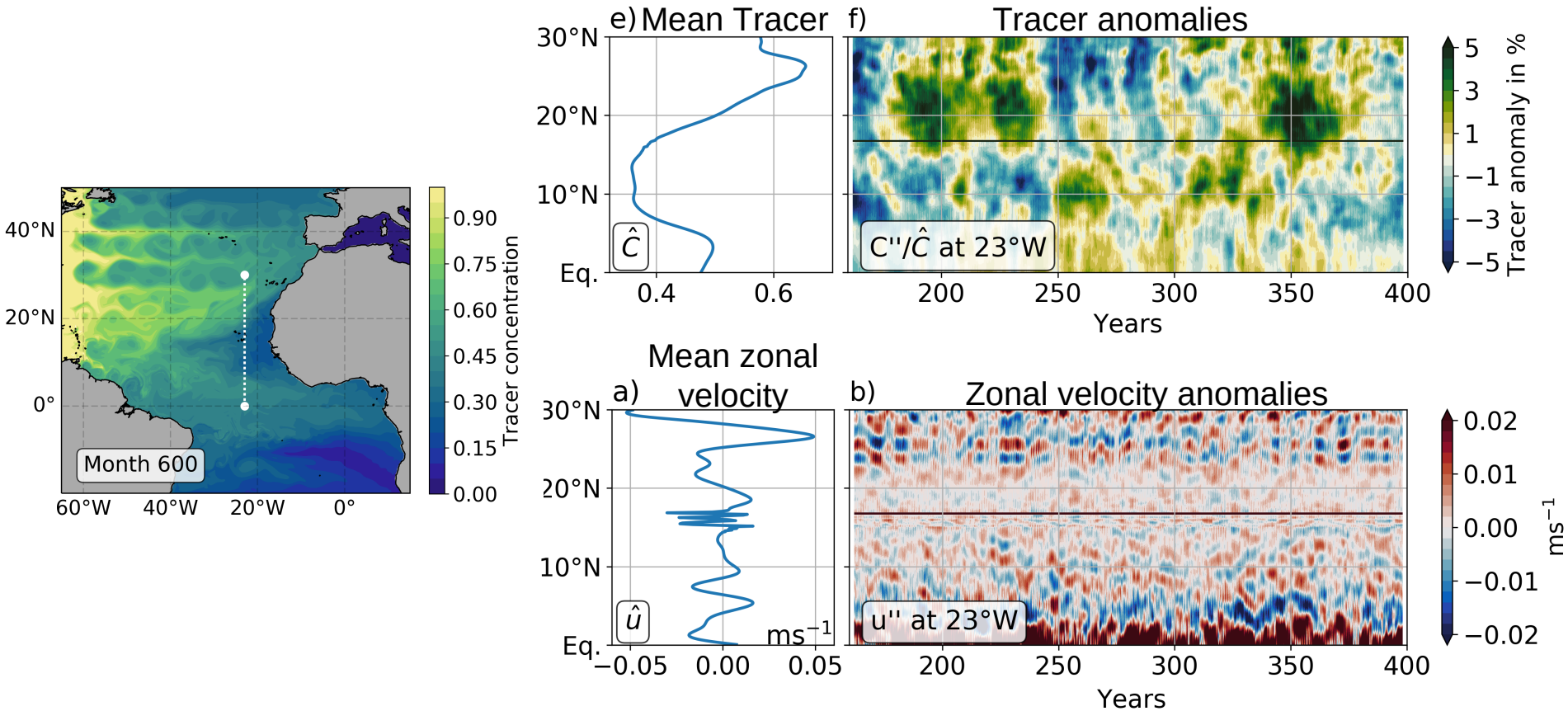
Tracer variability in the Atlantic basin



➔ interannual to decadal tracer variability is excited off the equator by an annual period forcing



Connection between tracer variability and zonal velocity



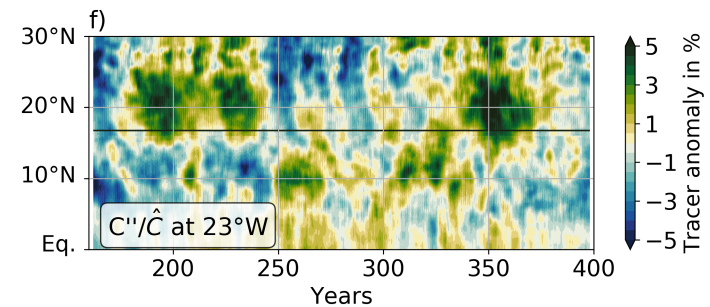
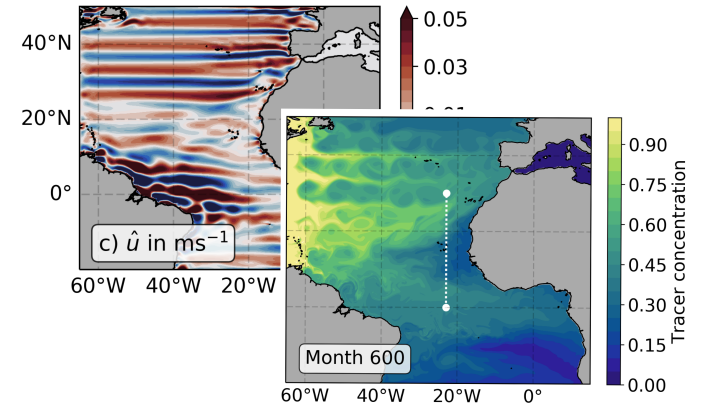
➔ multi-decadal tracer variability is accompanied by (multi-)decadal jet variability

Summary & Outlook

➔ the annually forced shallow water model features LAZJs, rectified by eddies and Rossby waves, that ventilate a more or less realistic ETNA OMZ

➔ inter-annual to multi-decadal variability of the tracer concentration is generated - it is accompanied by (multi-)decadal jet variability

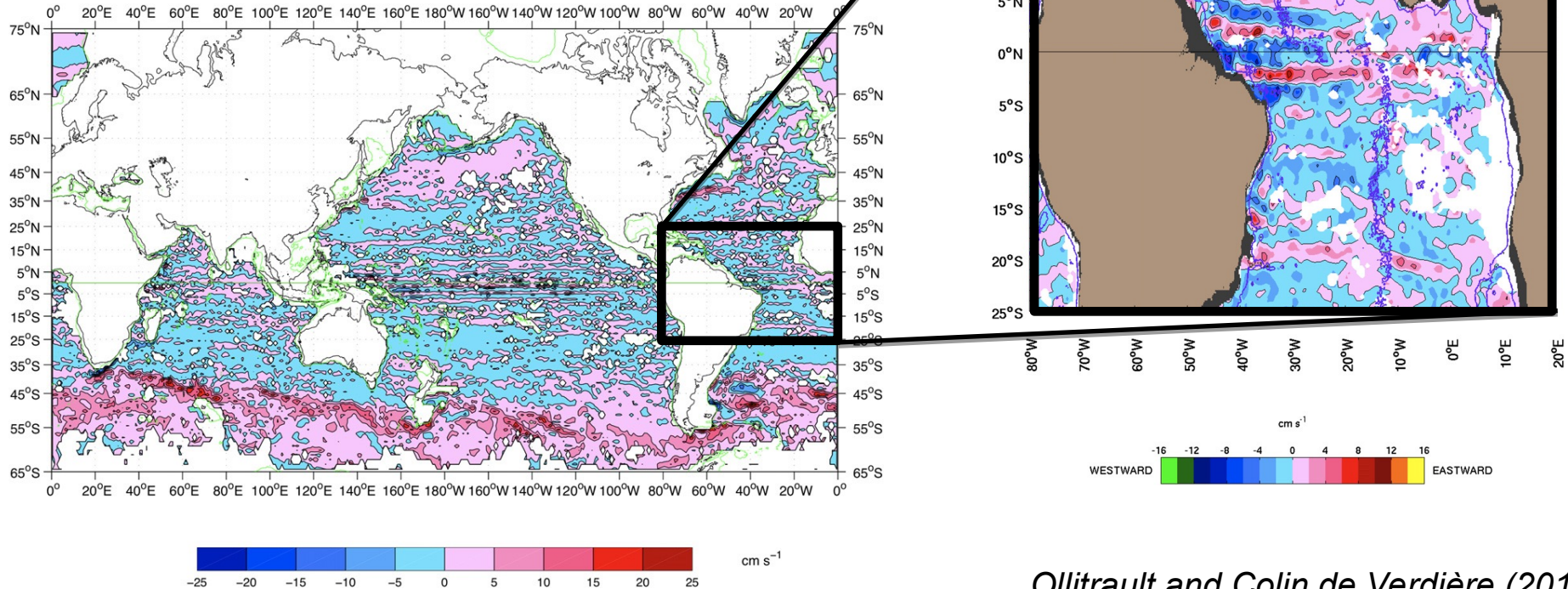
➔ obtain better understanding by turning to a more realistic model set-up (multi-layer model or GCM) and/or increasing the forcing complexity



Appendix

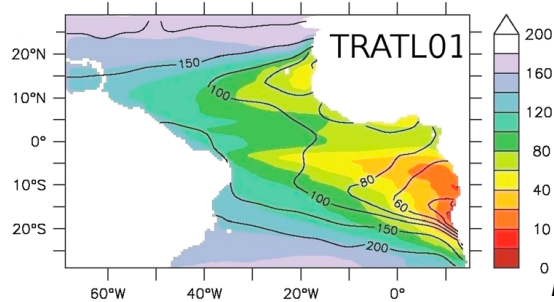
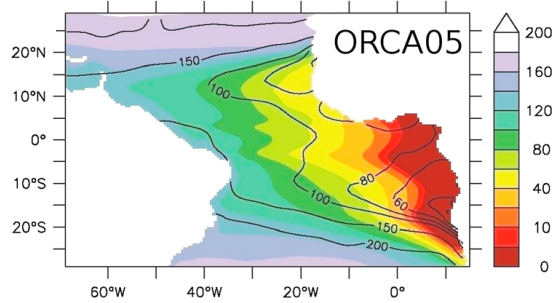
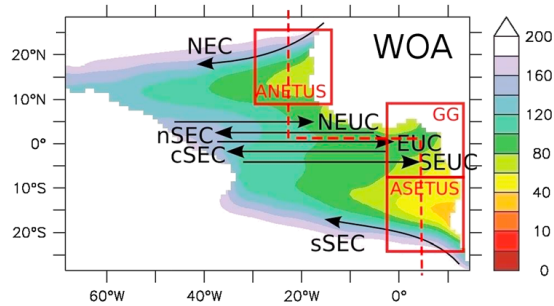
Latitudinally alternating zonal jets (LAZJs)

Zonal velocity at ~1000m depth



Ollitrault and Colin de Verdière (2014)

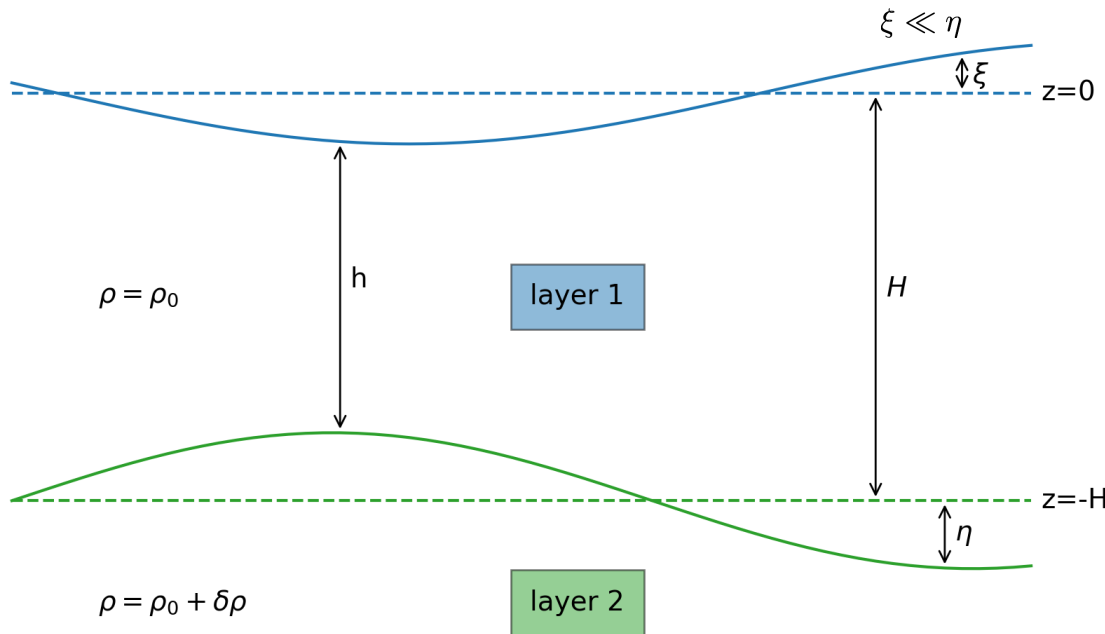
Modelling the ETNA OMZ



Duteil et al. (2014)

- so far no good understanding of the long term variability of the ETNA OMZ
- Mesoscale dynamics play an important role in the ventilation of the ETNA OMZ
- Turn to a non-linear shallow water model coupled to an advection-diffusion model to get a conceptual understanding

Non-linear shallow water model



- Dynamical equations:

$$\frac{\partial u}{\partial t} = ghv - \frac{1}{r \cos \theta} \frac{\partial E}{\partial \lambda} + M_u + F_u$$

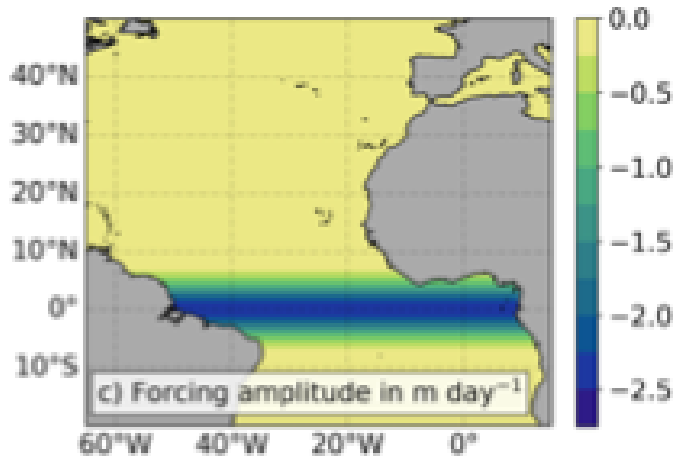
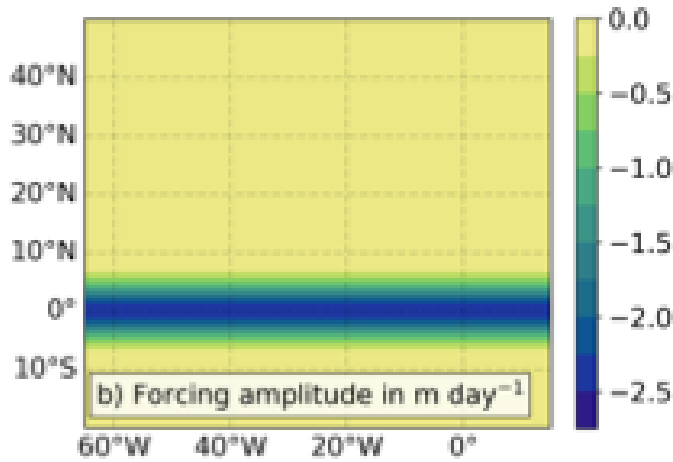
$$\frac{\partial v}{\partial t} = -ghu - \frac{1}{r} \frac{\partial E}{\partial \theta} + M_v + F_v$$

$$\frac{\partial \eta}{\partial t} = -\frac{1}{r \cos \theta} \left(\frac{\partial (hu)}{\partial \lambda} + \frac{\partial (hv \cos \theta)}{\partial \theta} \right) + F_\eta$$

- 1.5 layers - infinitely deep lower layer with vanishing velocities

- set to represent the first baroclinic mode with $c = 2.7 \text{ ms}^{-1}$ ($H=500 \text{ m}$, $g' = 1.5 \cdot 10^{-2} \text{ ms}^{-2}$)

Non-linear shallow water model



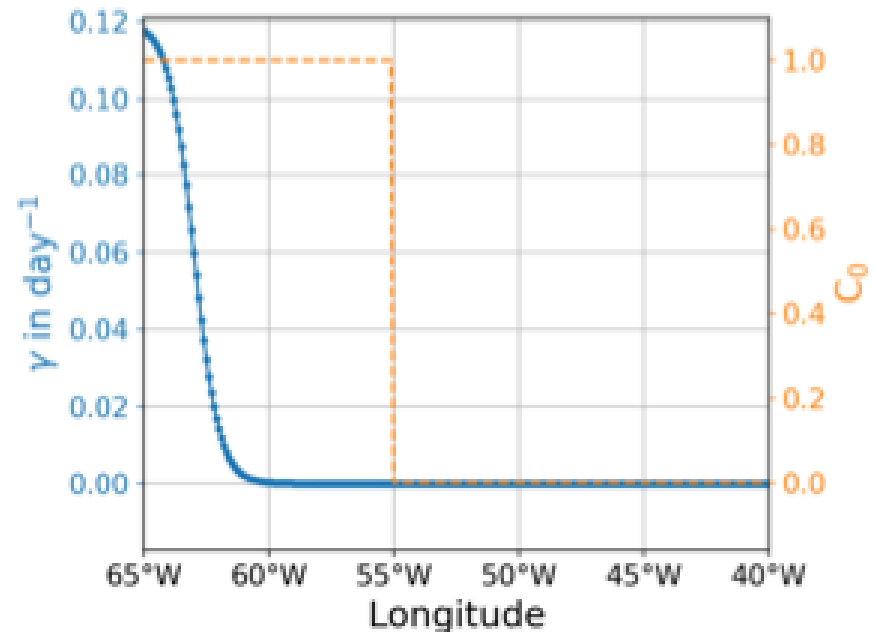
- rectangular and Atlantic basin (20°S-50°N, 65°W-15°E)
- 0.1° resolution
- viscosity set to 100 m²s⁻¹
- run with no-slip boundary conditions
- annual period forcing

$$\begin{aligned} \frac{\partial u}{\partial t} &= qhv - \frac{1}{r \cos \vartheta} \frac{\partial E}{\partial \lambda} + M_u + \cancel{F_u} \\ \frac{\partial v}{\partial t} &= -qhu - \frac{1}{r} \frac{\partial E}{\partial \vartheta} + M_v + \cancel{F_v} \\ \frac{\partial \eta}{\partial t} &= -\frac{1}{r \cos \vartheta} \left(\frac{\partial (hu)}{\partial \lambda} + \frac{\partial (hv \cos \vartheta)}{\partial \vartheta} \right) + \boxed{F_\eta} \end{aligned}$$

Advection-diffusion model

$$\underbrace{\frac{\partial(Ch)}{\partial t}}_1 + \underbrace{\nabla \cdot (Ch\mathbf{u})}_2 = \underbrace{\nabla \cdot (\kappa_h h \nabla C)}_3 - \underbrace{JCh}_4 - \underbrace{h\gamma(C - C_0)}_5 + \underbrace{CF_0}_6$$

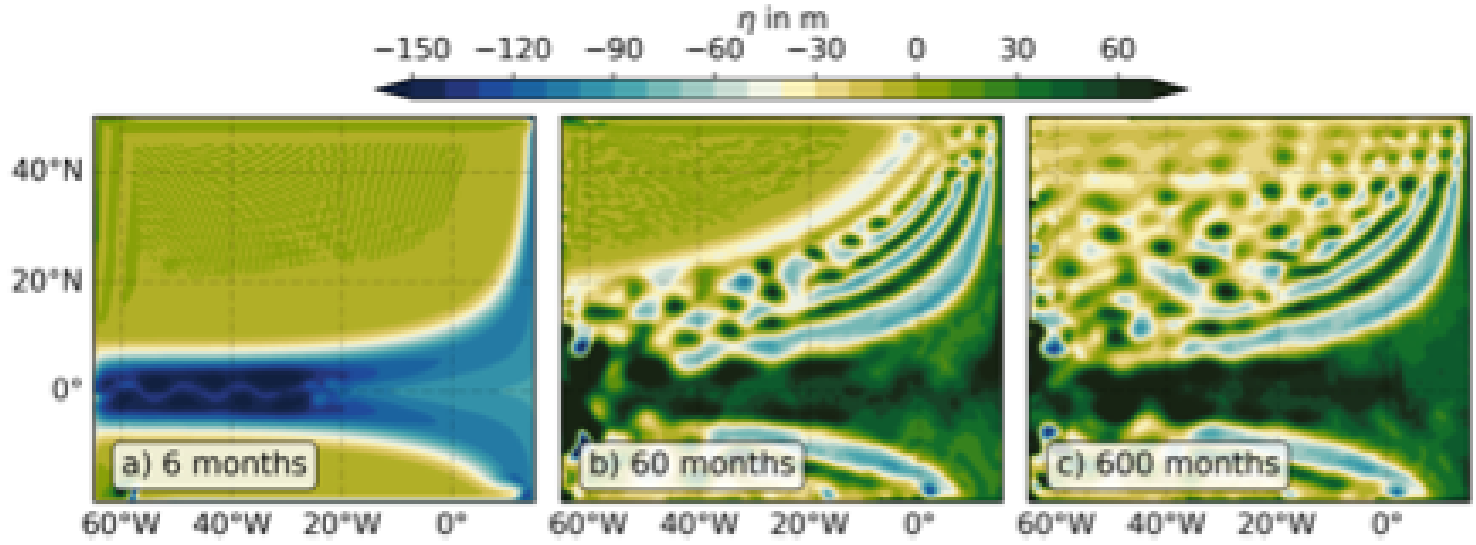
- 1.tendency
- 2.advective terms
- 3.diffusion
- 4.tracer sink (consumption,
 $J \approx 1/49 \text{ year}^{-1}$)
- 5.tracer source
(relaxation at western boundary,
 $\gamma_0 \approx 1/8 \text{ day}^{-1}$)
- 6.forcing



 **Tracer set-up to mimic oxygen**

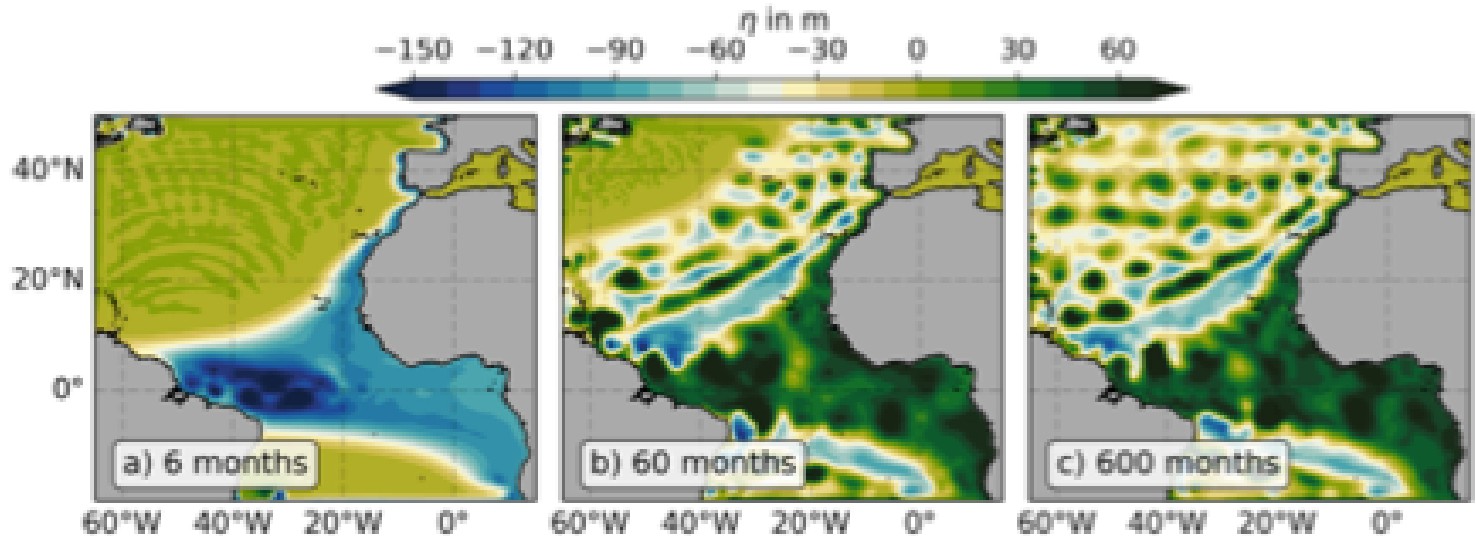
Spin-up

Interface displacement

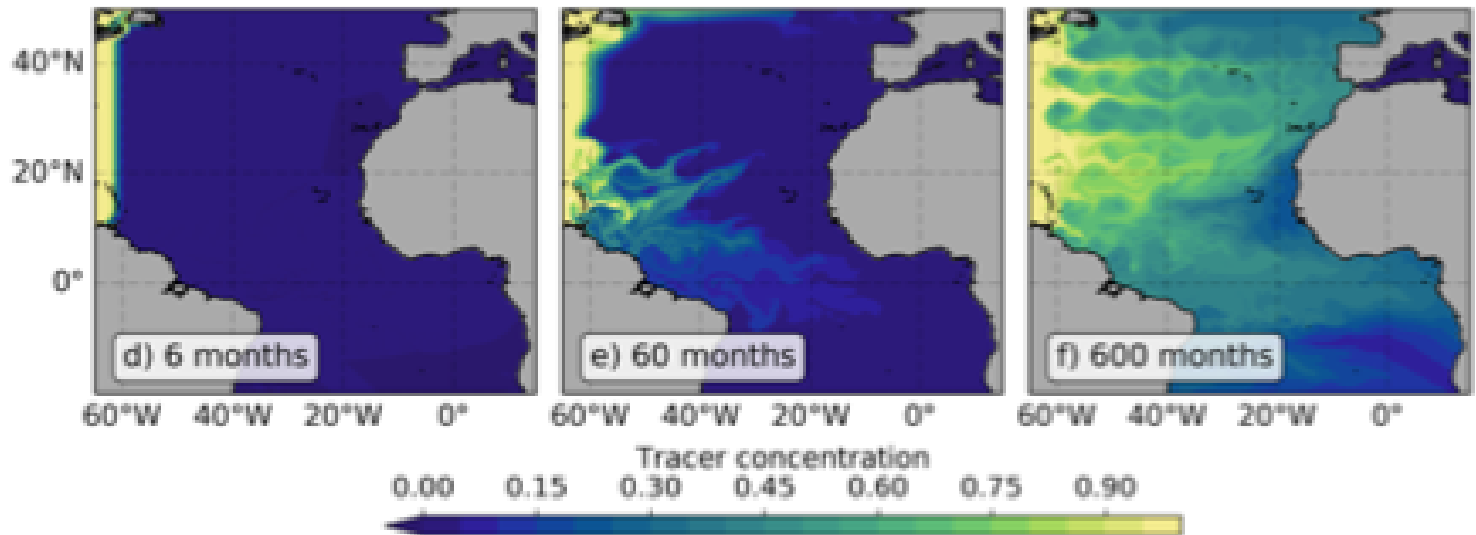


Spin-up

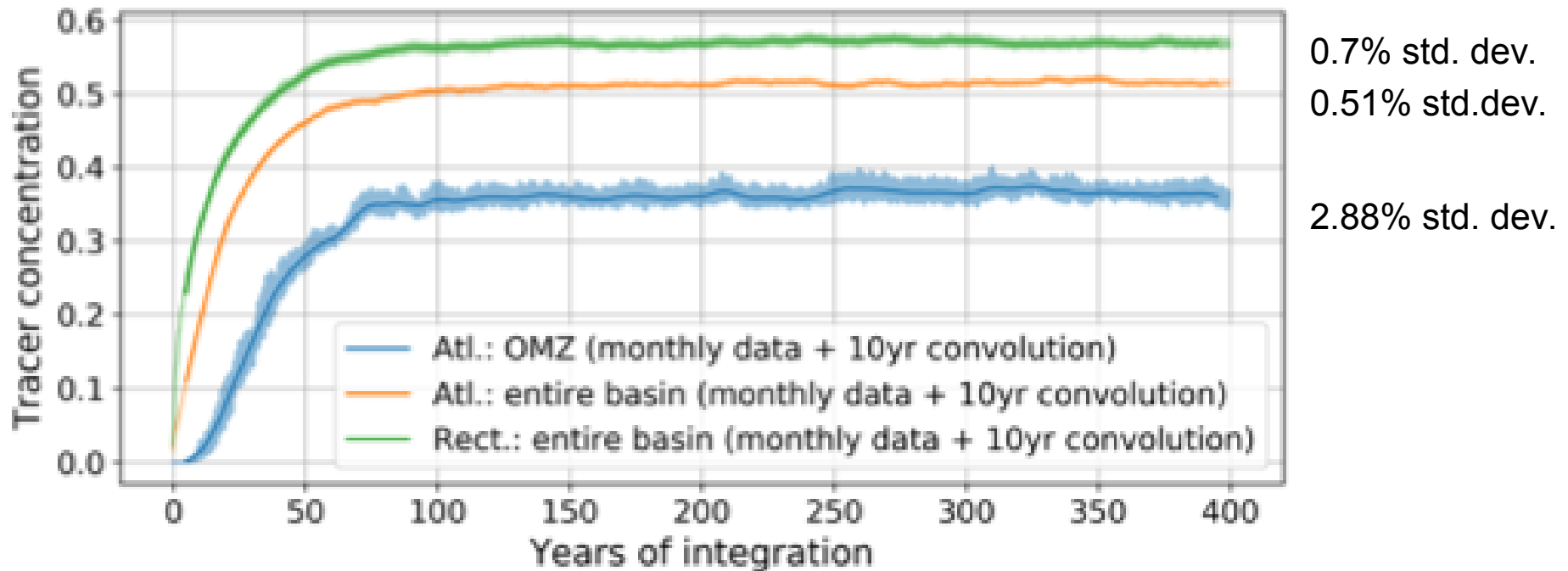
Interface displacement



Tracer concentration



Spin-up - Tracer content



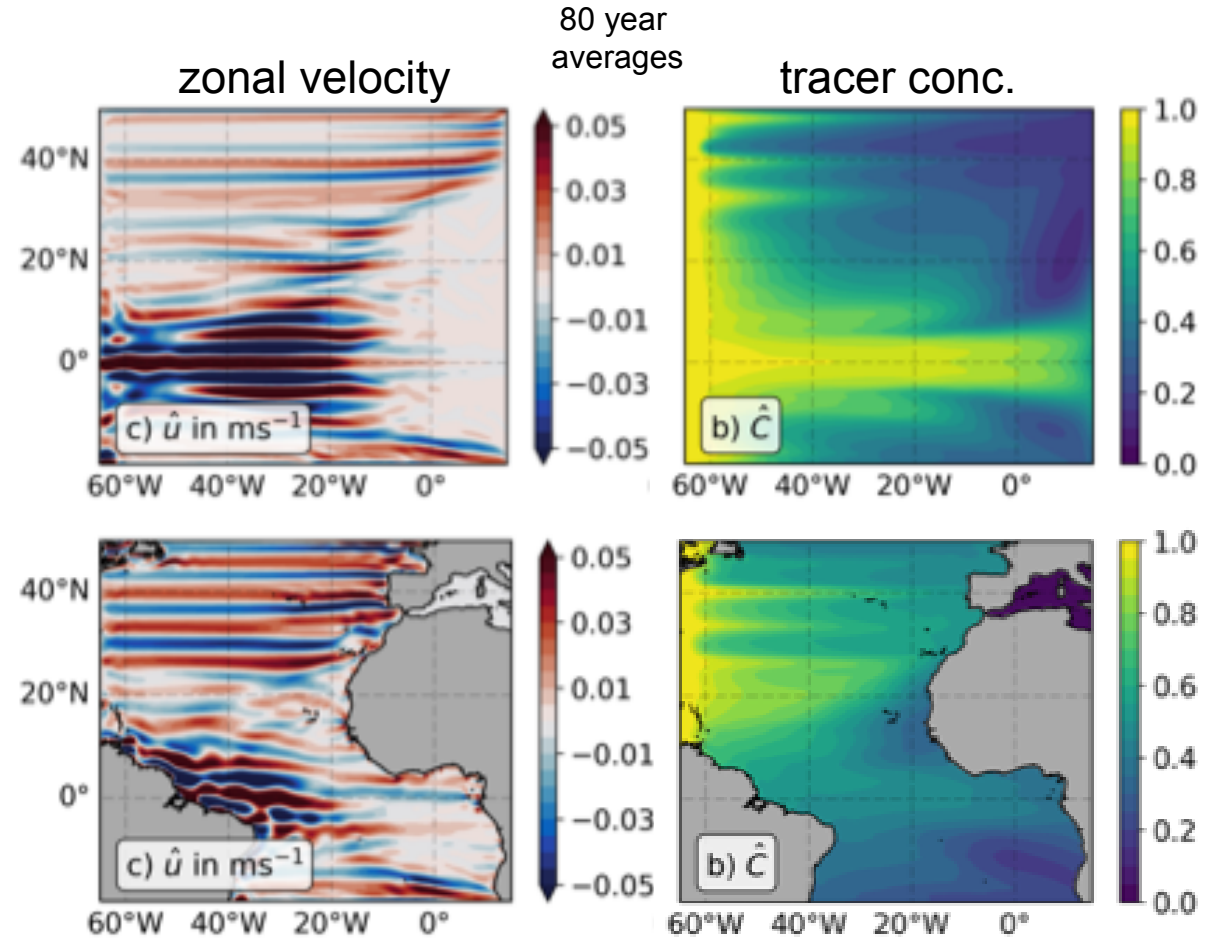
Statistical mean state

Thickness weighted average:

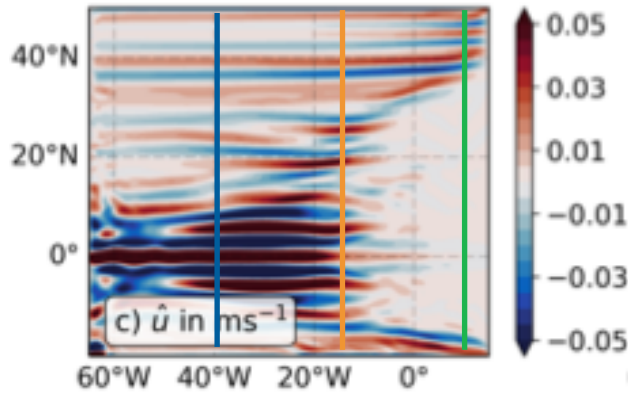
$$\hat{\alpha} = \frac{\overline{\alpha h}}{\overline{h}}$$

Rectangular basin

Atlantic basin

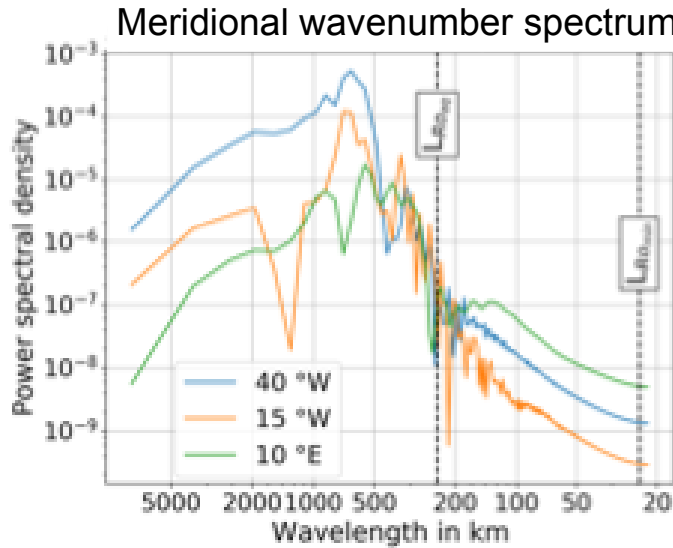


Meridional width of zonal jets

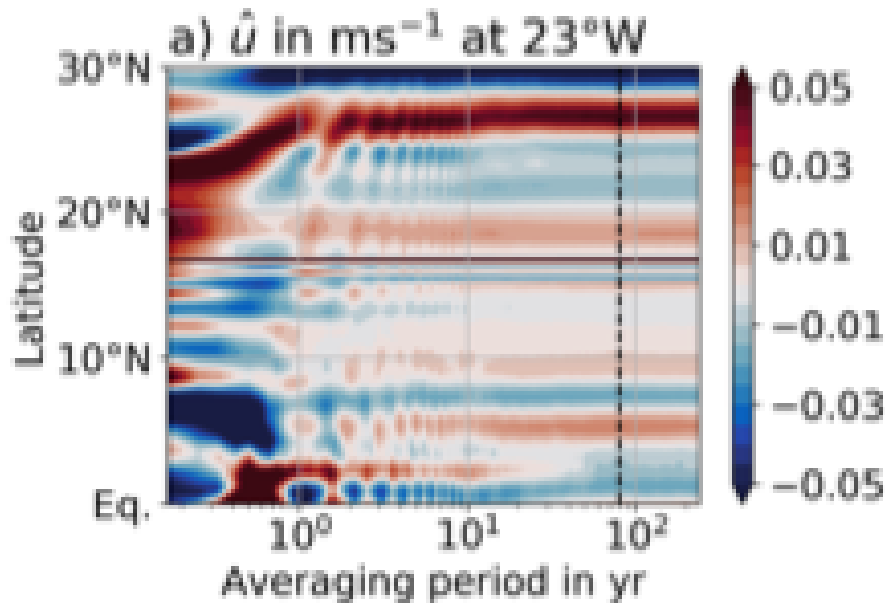


Rossby radius: $L_{R\Omega} = \frac{(g'H)^{1/2}}{f}$, $L_{R\alpha} = \left(\frac{c}{2\beta}\right)^{1/2}$

- zonal jets are wider than both:
 1. Rossby radius
 2. Rhines scale



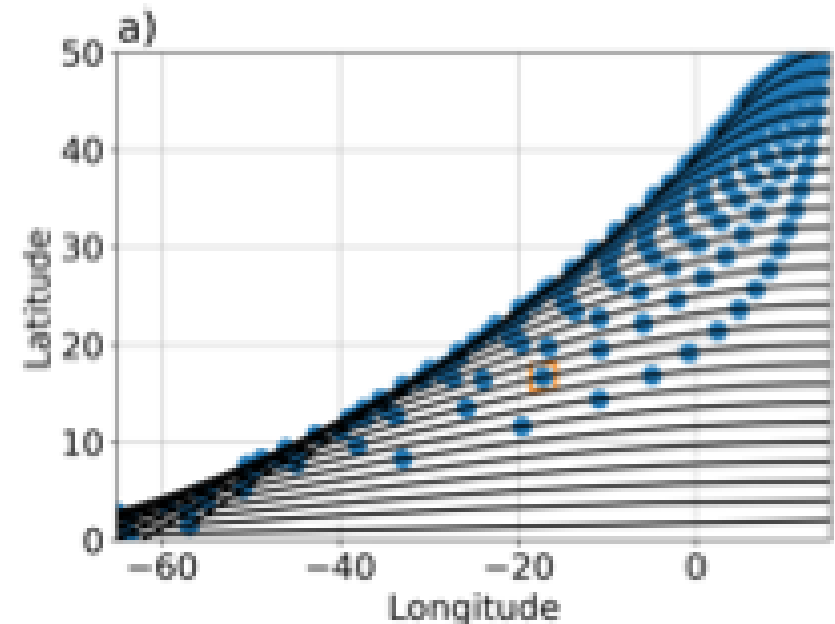
Meridional width of zonal jets



- eddies rectify the zonal jets
- hence, the eddy formation process plays a large role in setting the meridional width of the jets
- Resonant triad instability has been suggested to lead to break up of Rossby wave fronts (Qiu et al., 2013)

Zonal jet width - Non-linear triad instability

- Rossby wave ray theory (Schopf, 1981)
 - equatorial β -plane
 - purely meridional eastern boundary
 - initially vanishing meridional wavenumber
- dispersion relation:
$$\omega = \frac{-\beta k}{(k^2 + l^2 + f^2 c^{-2})}$$
- the β -dispersion leads to the formation of the caustic
- along the ray paths, the triad instability mechanism can be analysed following Pedlosky (1987) and Qiu et al. (2013)



Zonal jet width - Non-linear triad instability

- for a resonant triad, three Rossby waves are required that fulfil the following condition:

$$k_1 + k_2 + k_3 = 0$$

$$l_1 + l_2 + l_3 = 0$$

$$\omega_1 + \omega_2 + \omega_3 = 0$$

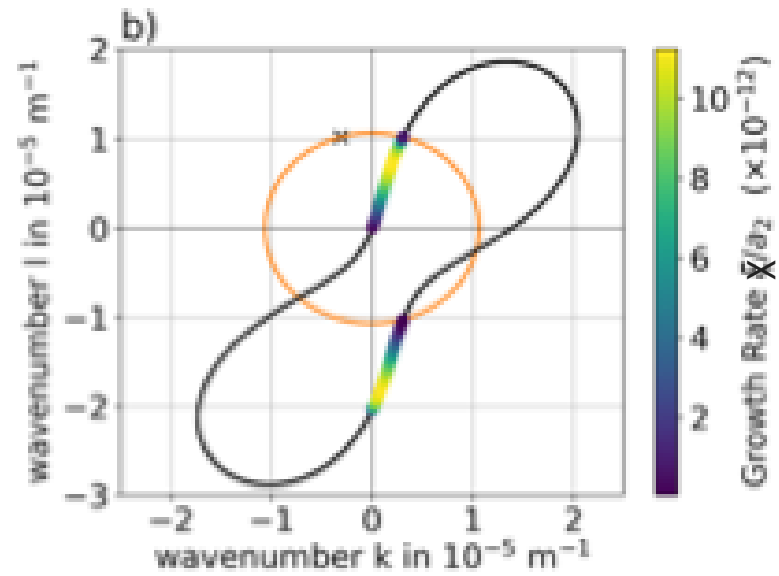
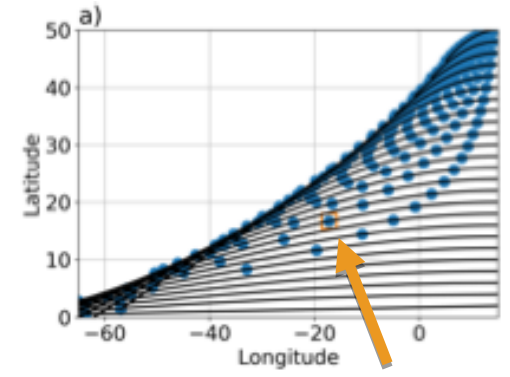
- assuming k_2, l_2, ω_2 etc. to be associated with the primary wave, the necessary instability criterion is given by $K_1 < K_2 < K_3$

- the growth rate for the secondary waves is given by:

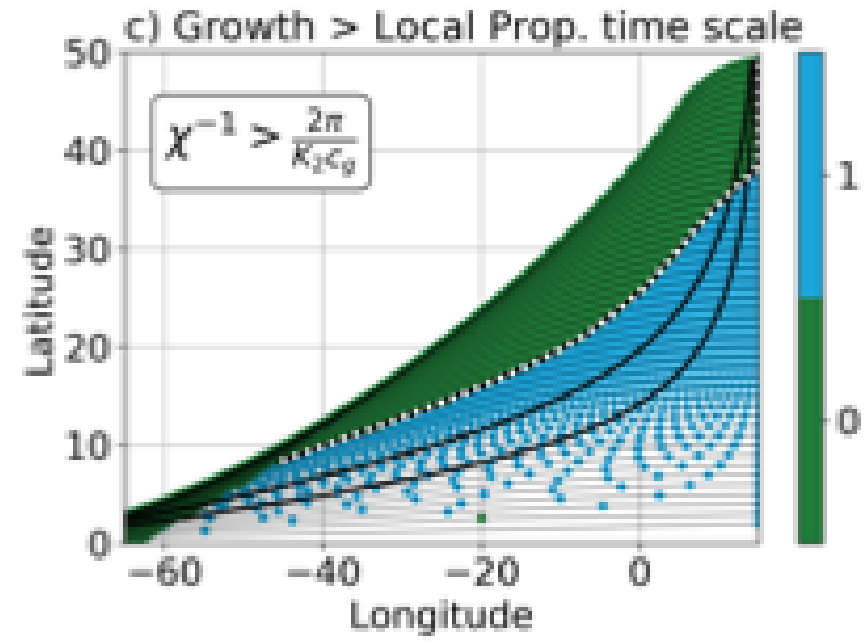
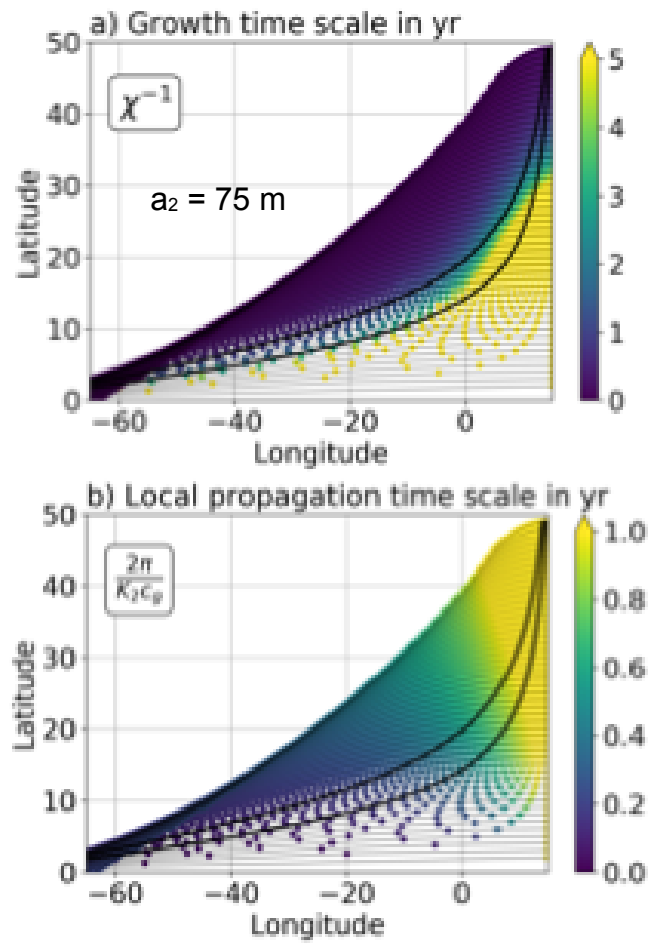
$$\chi = a_2 \left[\frac{B(K_2, K_3)B(K_1, K_2)}{(K_1^2 + f^2c^{-2})(K_3^2 + f^2c^{-2})} \right]^{1/2}$$

$$B(K_m, K_n) = (K_m^2 - K_n^2)(k_m l_n - k_n l_m)$$

with

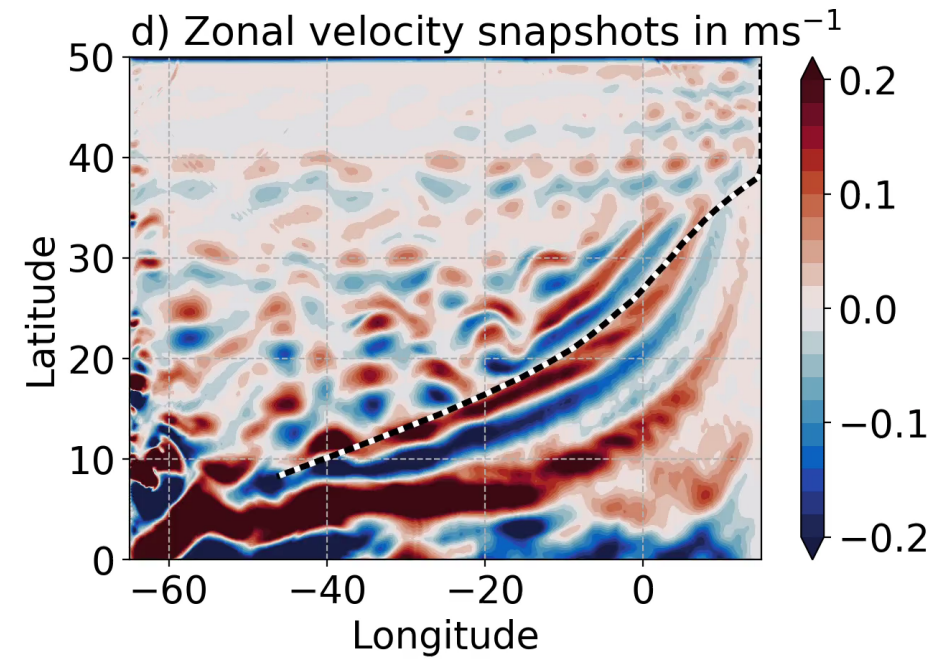
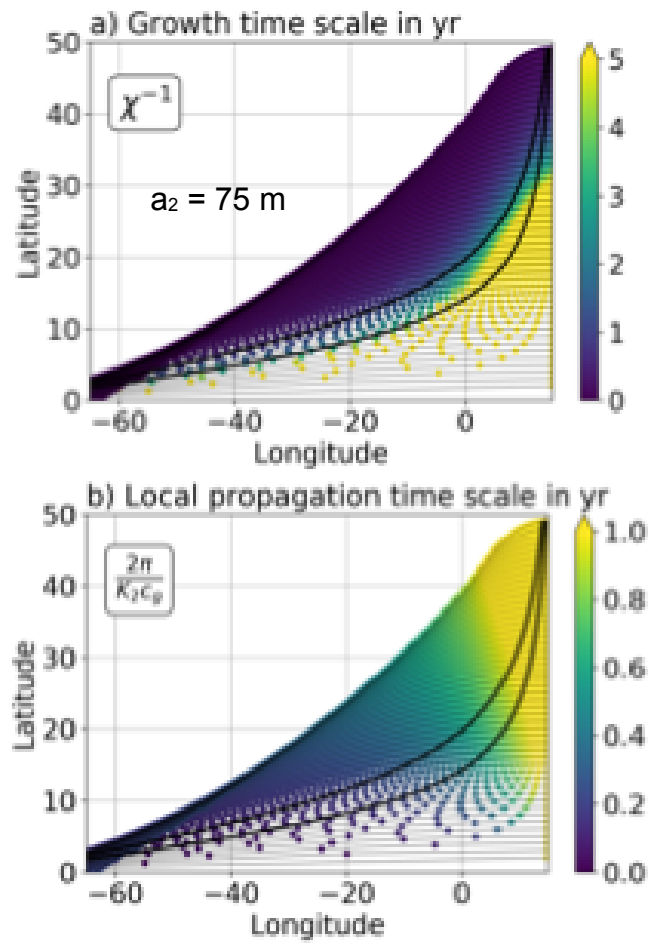


Zonal jet width - Non-linear triad instability



Physically one can expect the breakdown to occur where $\chi^{-1} = \frac{2\pi}{K_2 c_g}$

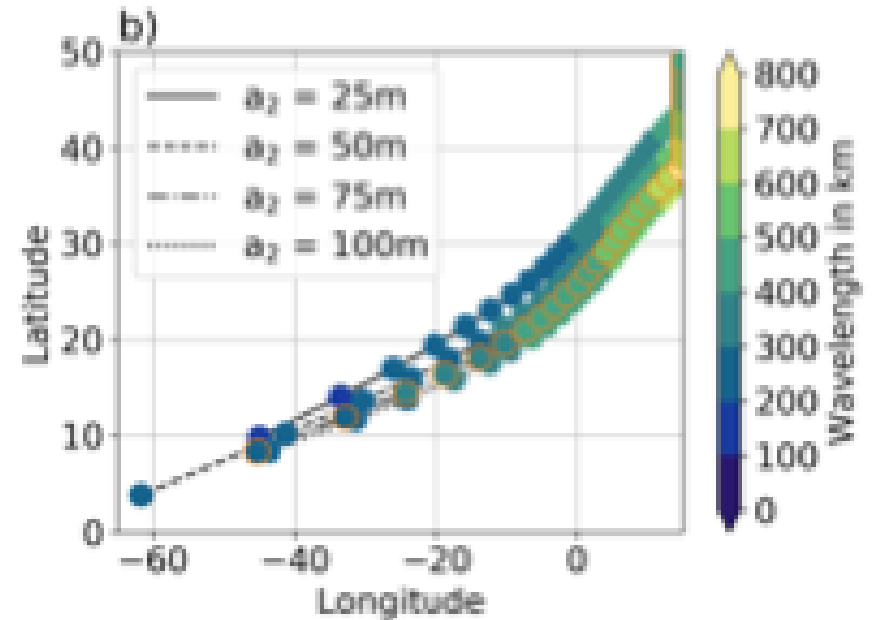
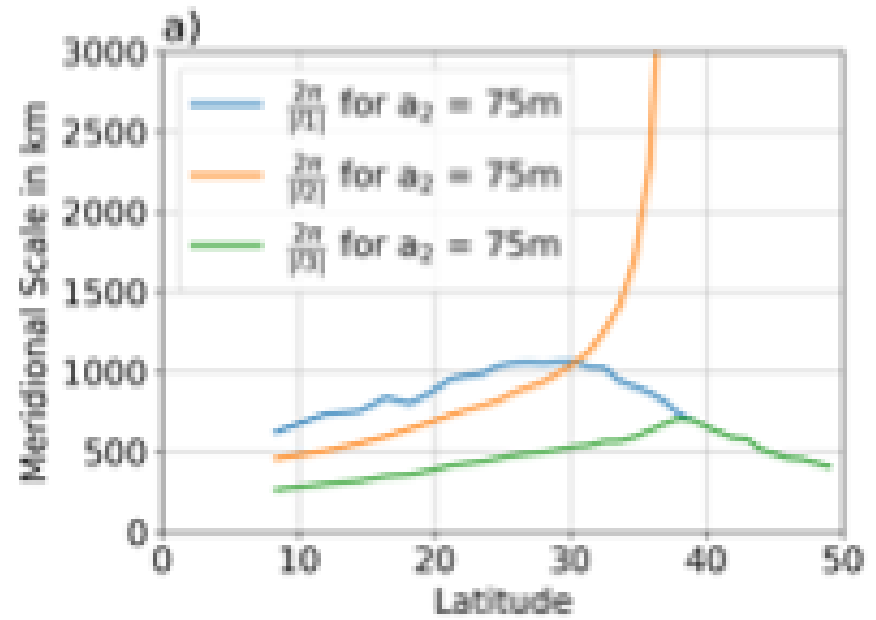
Zonal jet width - Non-linear triad instability



Projection onto the modelled field in spherical coordinates

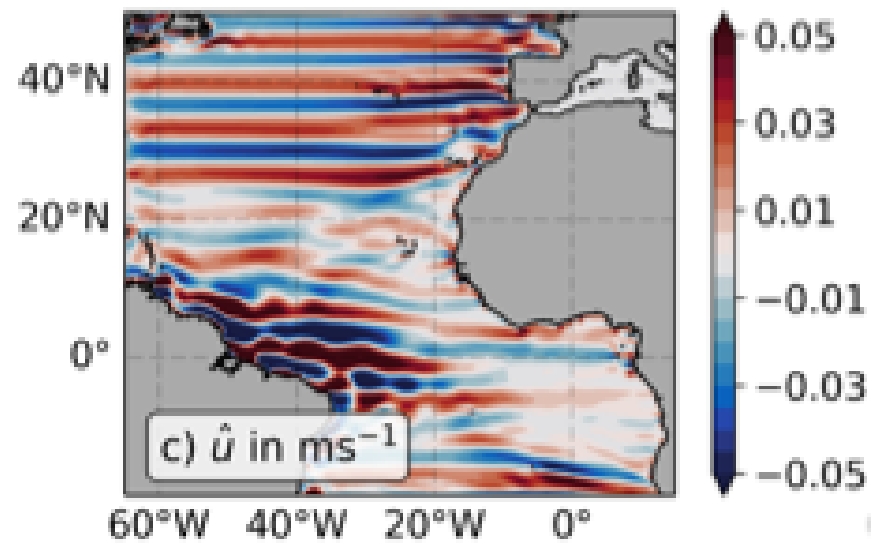
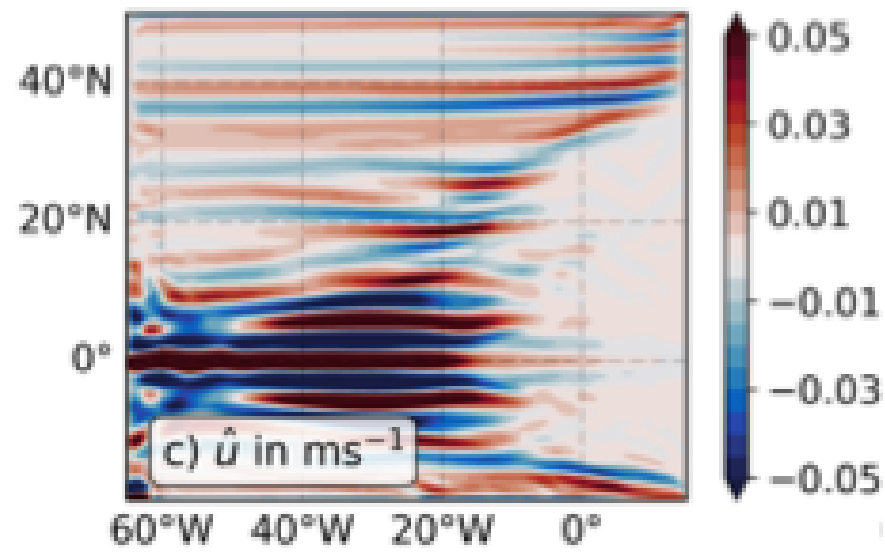
Zonal jet width - Non-linear triad instability

$$\chi = a_2 \left[\frac{B(K_2, K_3)B(K_1, K_2)}{(K_1^2 + f^2c^{-2})(K_3^2 + f^2c^{-2})} \right]^{1/2}$$



- inter-annual modulation of primary Rossby wave strength could lead to variability in zonal jet strength, width and position

Zonal jets - origin

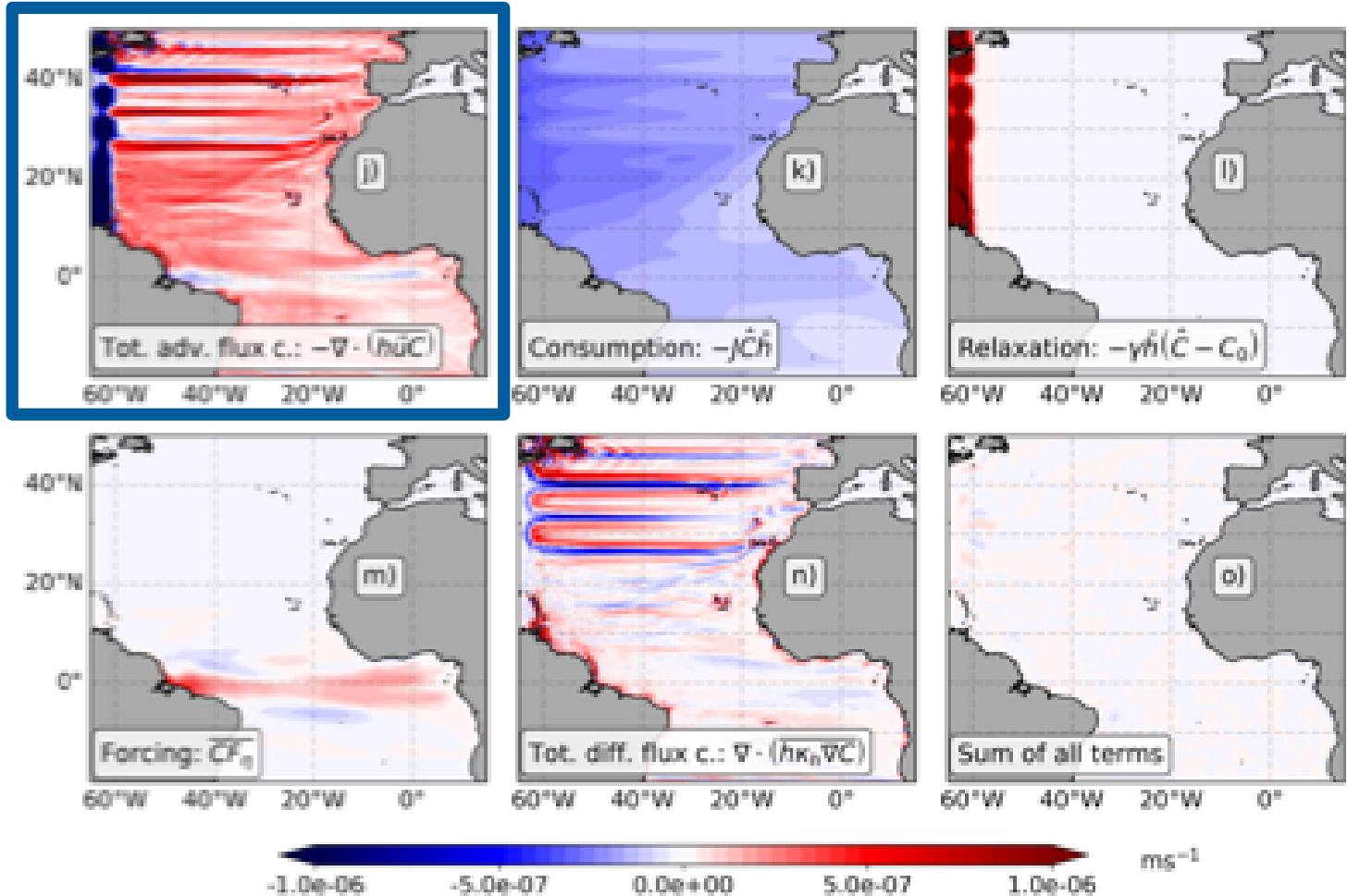


- zonal jets rectify through eddies after non-linear triad instability

- coastline has some effect on the jet generation - jets reach into ETNA OMZ

Tracer budget

$$\frac{\partial (\hat{C}h)}{\partial t} = -\nabla \cdot (\overline{Ch\mathbf{u}}) + \nabla \cdot (\overline{h\kappa_h \nabla C}) - J\hat{C}h - \gamma h (\hat{C} - C_0) + \overline{CF_\tau}$$



Thickness weighted average:
 $\hat{\alpha} = \frac{\overline{\alpha h}}{\overline{h}}$

Analysis of advective flux convergence

$$-\nabla \cdot (\overline{C\mathbf{u}}) = \text{mean flux convergence}$$

$$-\nabla \cdot (\overline{h\mathbf{u}'\hat{c}}) = \text{eddy flux c.}$$

$$-\nabla \cdot (\overline{h\mathbf{u}\hat{c}}) = -\nabla \cdot (\overline{h\mathbf{u}'\hat{c}}) - \nabla \cdot (\overline{h\mathbf{u}''\hat{c}''})$$

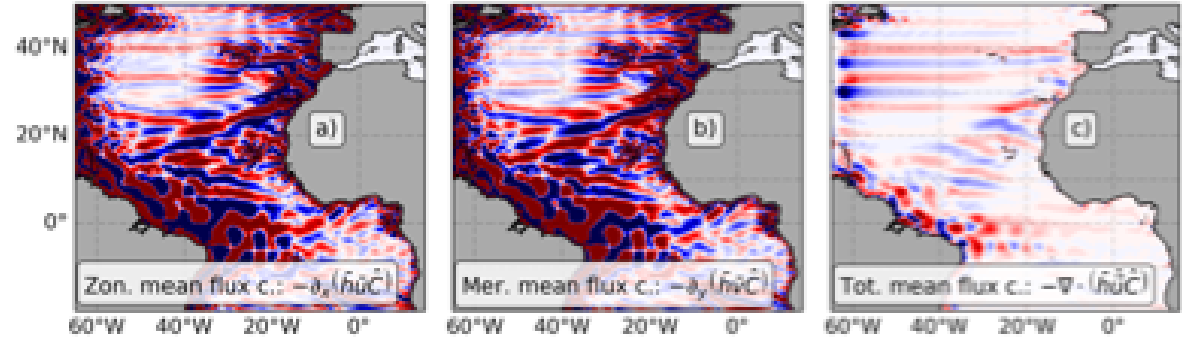
“eddy mixing”

with

$$\alpha = \hat{\alpha} + \alpha''$$

and bolus velocity $\overline{\mathbf{u}'h'}$

$$\mathbf{u}^* = \hat{\mathbf{u}} - \bar{\mathbf{u}} = \frac{\overline{\mathbf{u}'h'}}{\bar{h}}$$



Analysis of advective flux convergence

$$-\nabla \cdot (\overline{C\mathbf{h}\mathbf{u}}) = \text{mean flux convergence}$$

$$-\nabla \cdot (\overline{h\mathbf{u}'\hat{C}}) = \text{eddy flux c.}$$

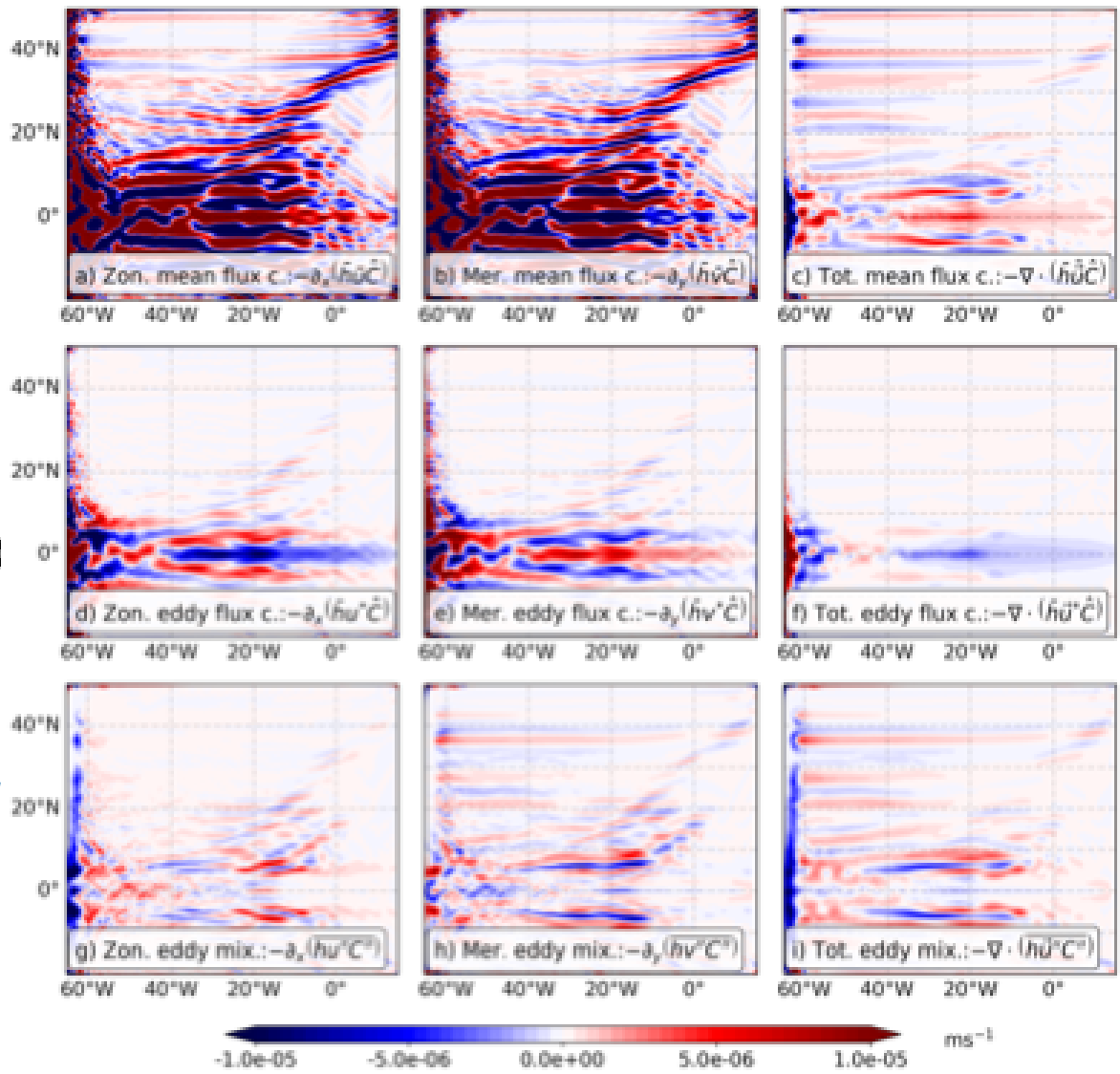
$$-\nabla \cdot (\overline{h\mathbf{u}'\hat{C}}) = \text{“eddy mixing”}$$

with

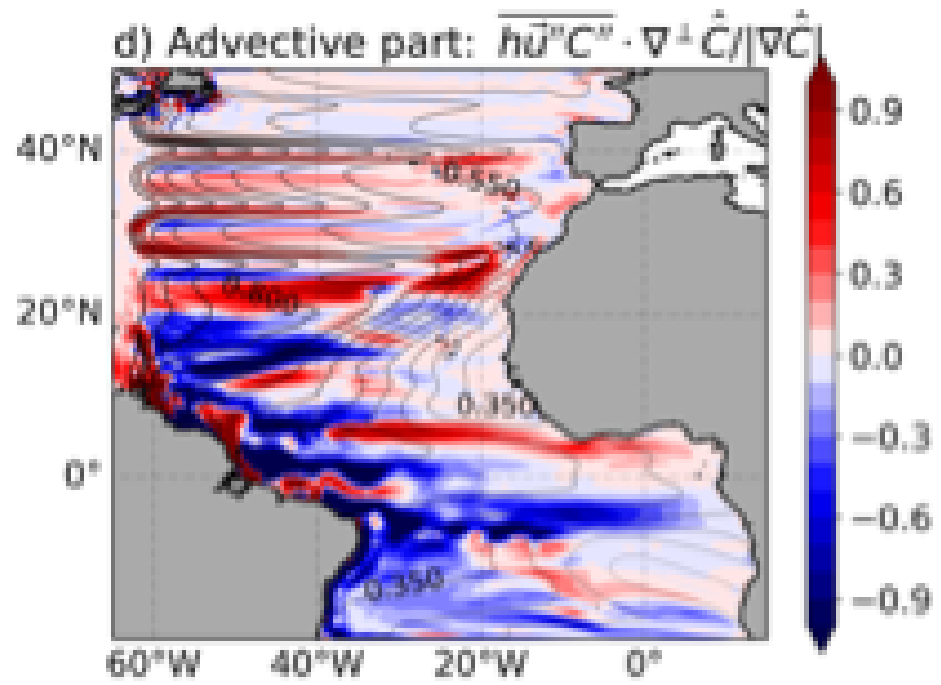
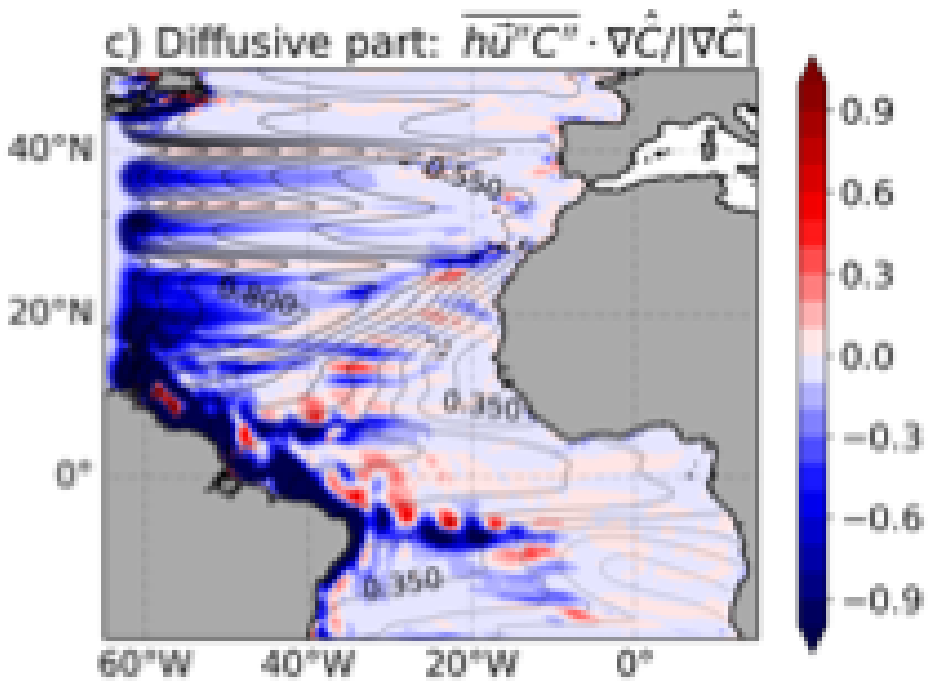
$$\alpha = \hat{\alpha} + \alpha''$$

and bolus velocity

$$\mathbf{u}^* = \hat{\mathbf{u}} - \overline{\mathbf{u}} = \frac{\mathbf{u}'h'}{\bar{h}}$$



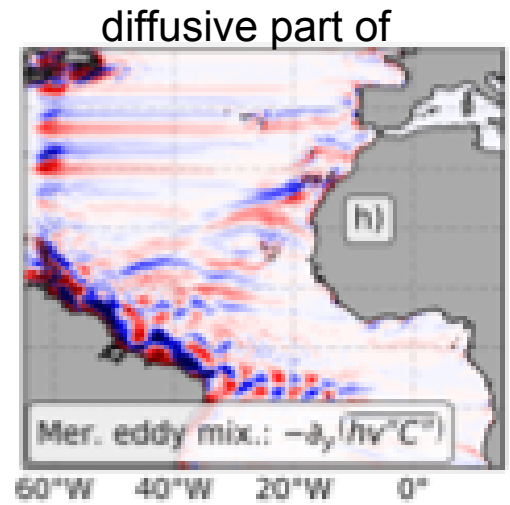
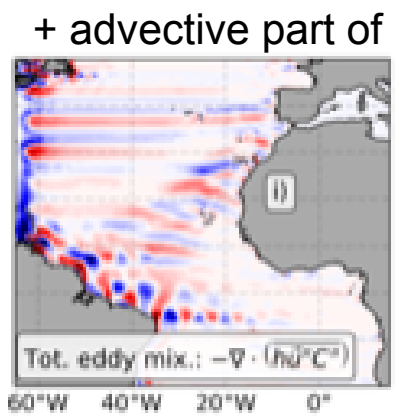
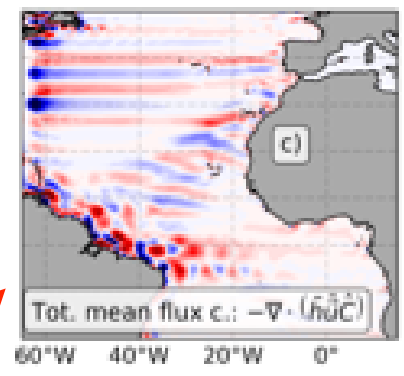
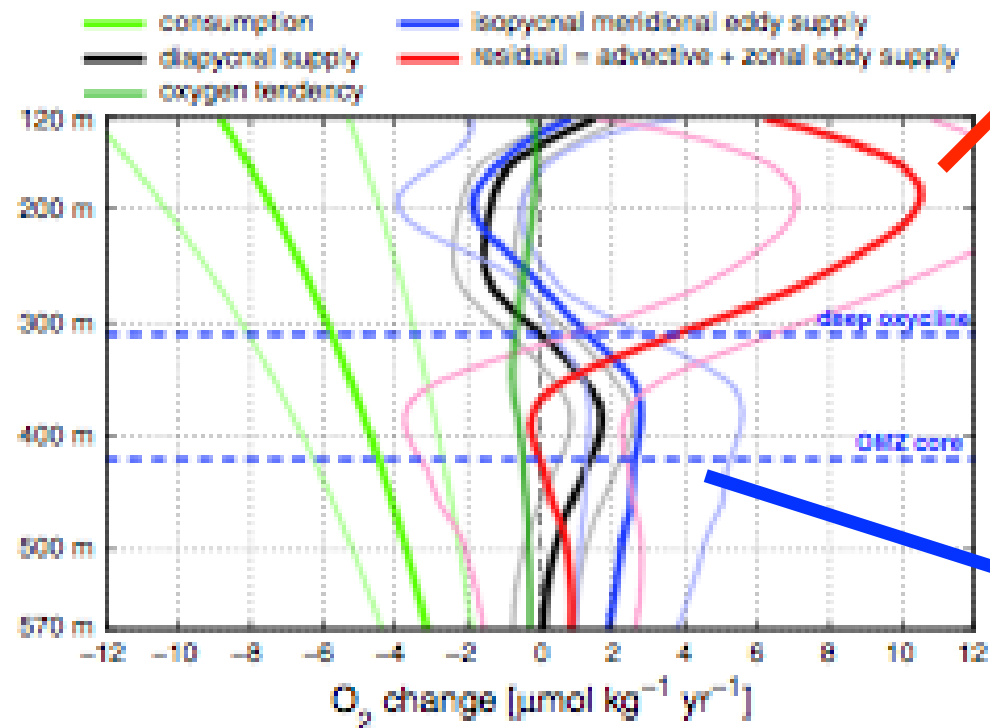
Nature of the “eddy mixing” term



- mostly down the tracer gradient
- i.e. a genuine diffusive flux

- along lines of equal tracer concentrations

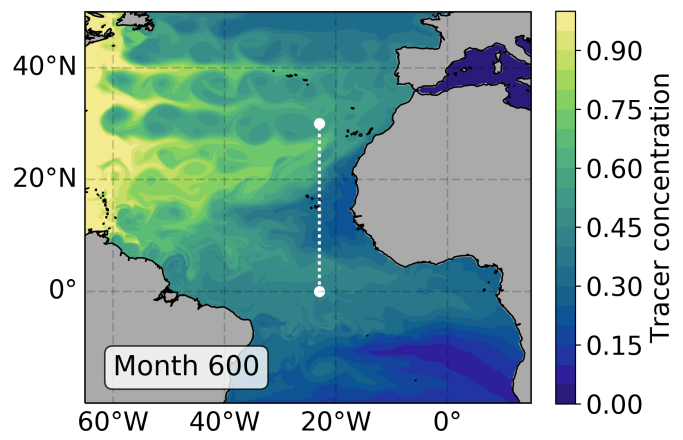
Budget of the ETNA OMZ at 23°W



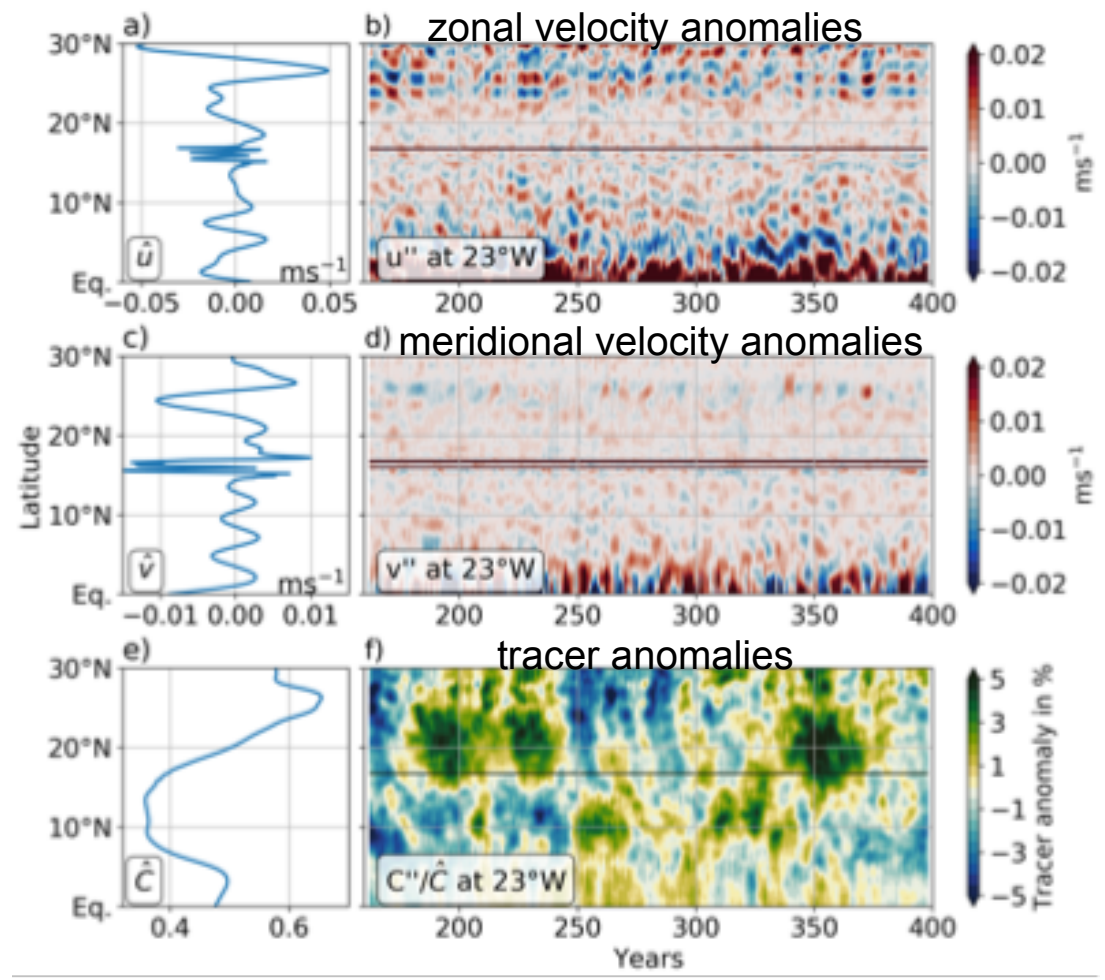
Hahn et al. (2014)

$$dOUR + O_{2,dia} + O_{2,y,eddy} + R_{O_2} = \partial_t O_2$$

Connection between zonal jet and tracer variability

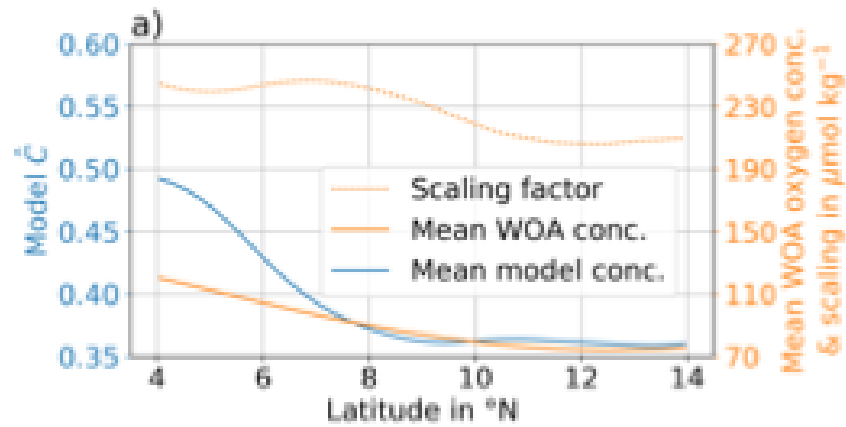


- interannual jet variability and interdecadal tracer variability are hard to link

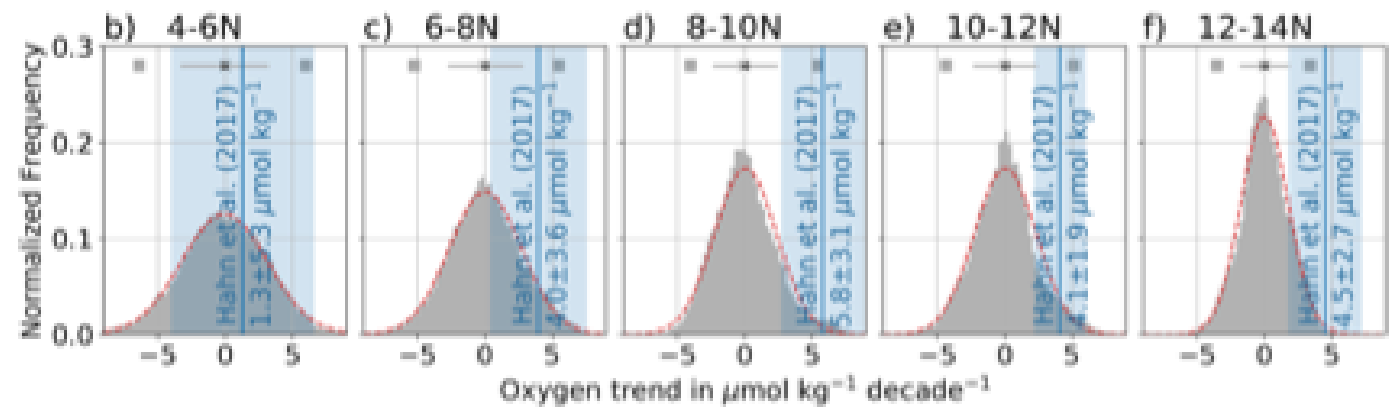


Comparison of modelled decadal trends at 23°W with observations

- scale modelled tracer concentrations to World Ocean Atlas concentrations using scaling factor

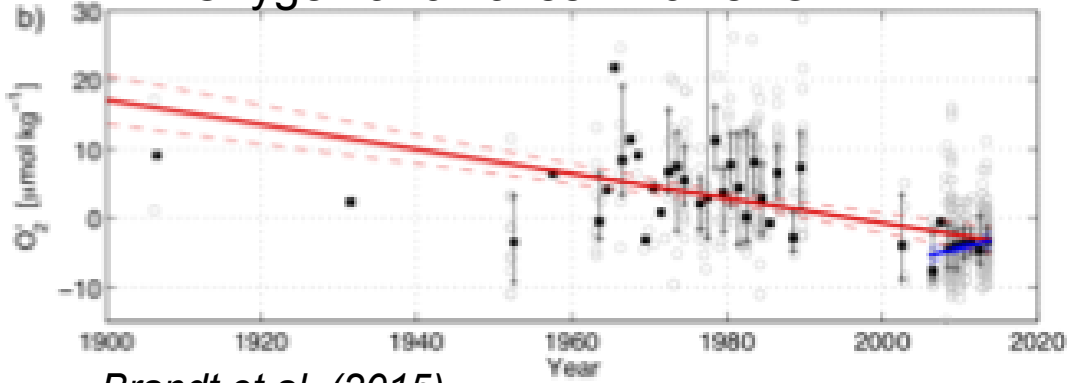


Observed decadal trends from Hahn et al. (2017) are possible realisations of modelled trends



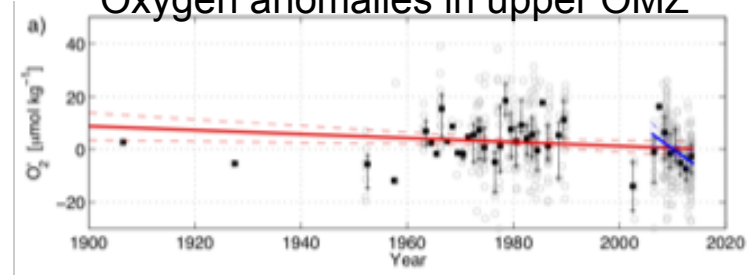
Compare trends for entire OMZ (9-15°N, 26-20°W)

Oxygen anomalies in lower OMZ

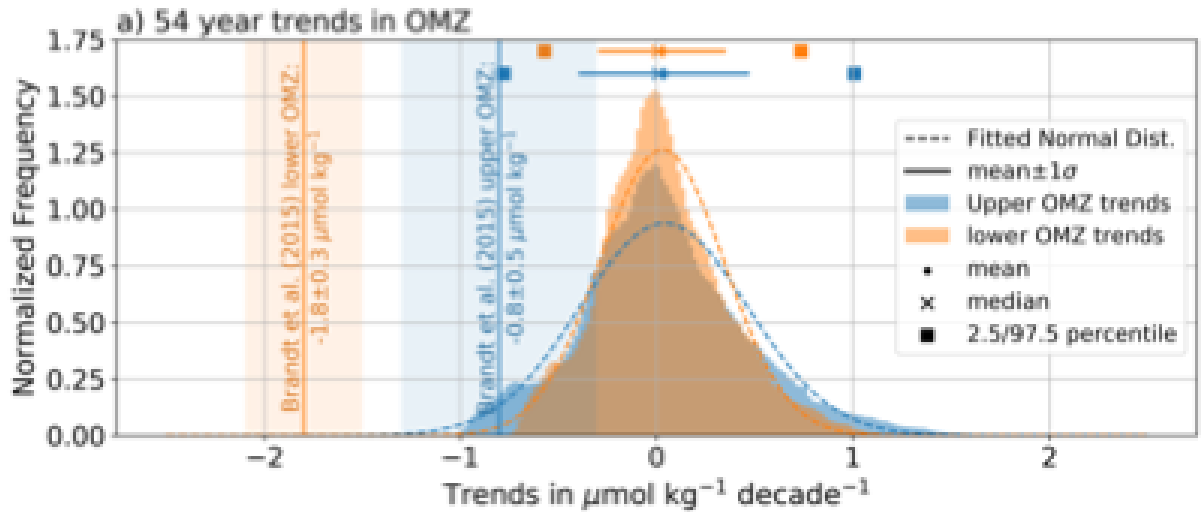


Brandt et al. (2015)

Oxygen anomalies in upper OMZ

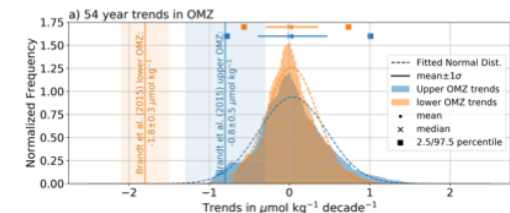
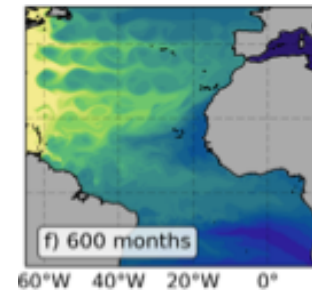
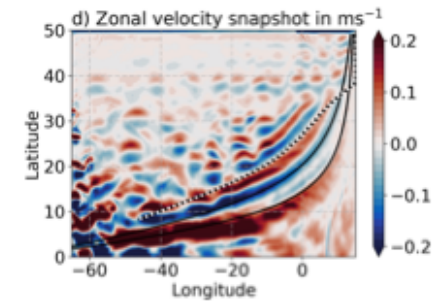
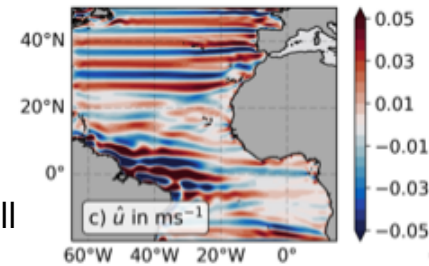


- Observed multi-decadal trends in lower OMZ are not captured by modelled tracer field

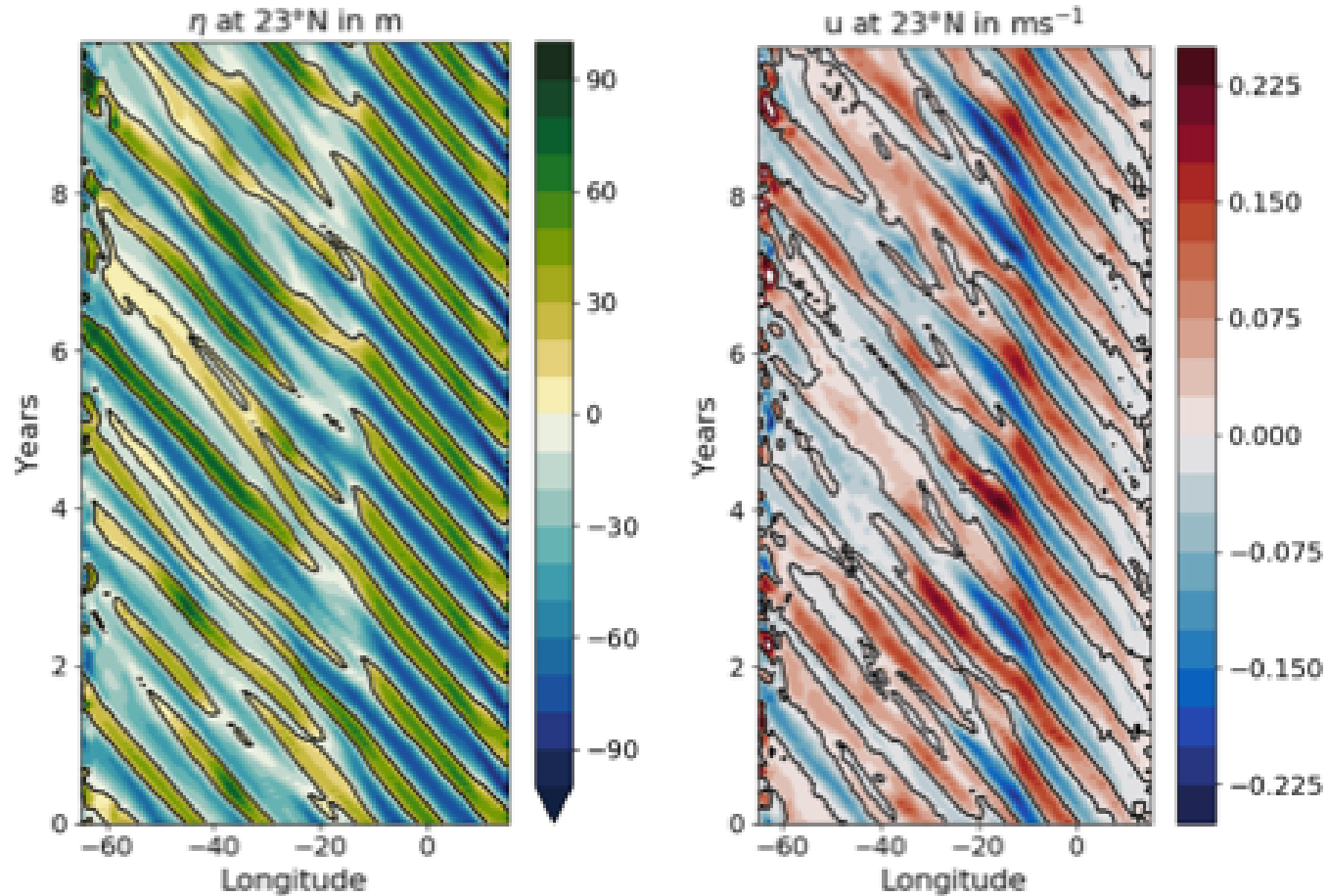


Summary

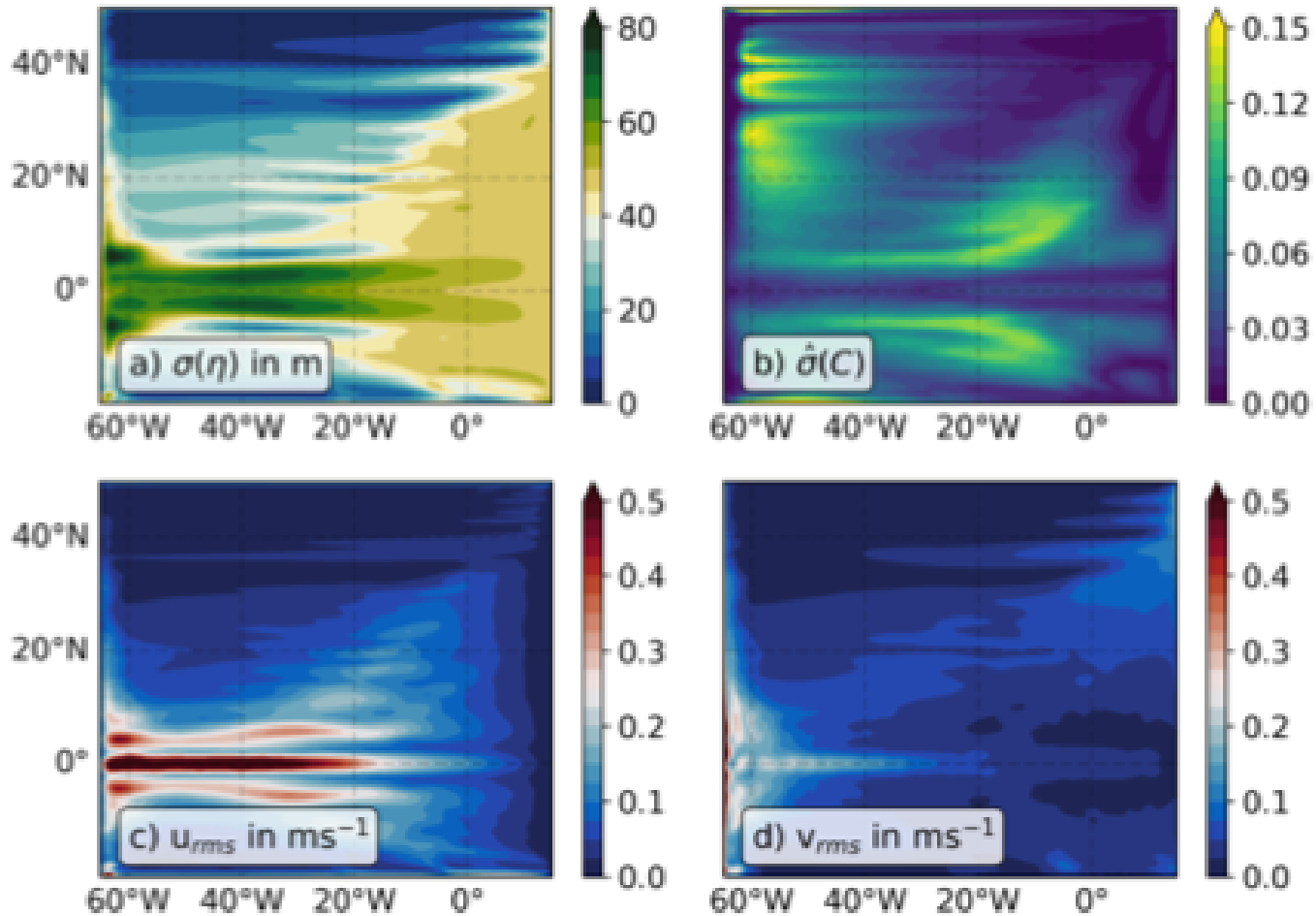
- the non-linear shallow water model is able to produce latitudinally alternating zonal jets by imposing an annual period forcing on the equator
- non-linear triad resonance is the likely Rossby wave front instability mechanism
- a more or less realistic “oxygen minimum zone” is established, which is mainly ventilated by a mean advective flux convergence and the meridional
- ~~interannual to interdecadal variability~~ component of the interannual variability of the tracer concentration is generated - the observed long term decrease in oxygen is however not reproduced



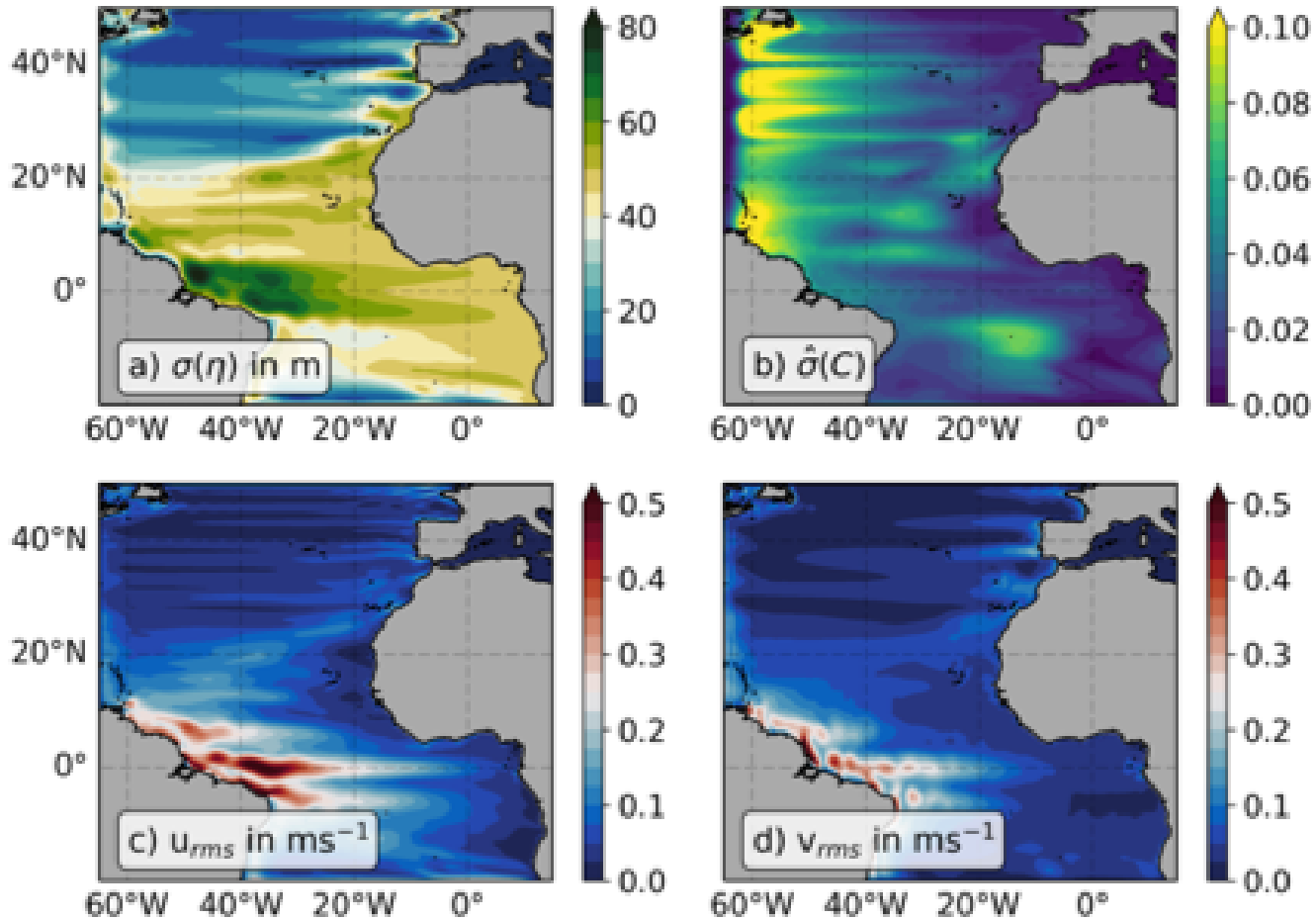
Zonal eddy propagation



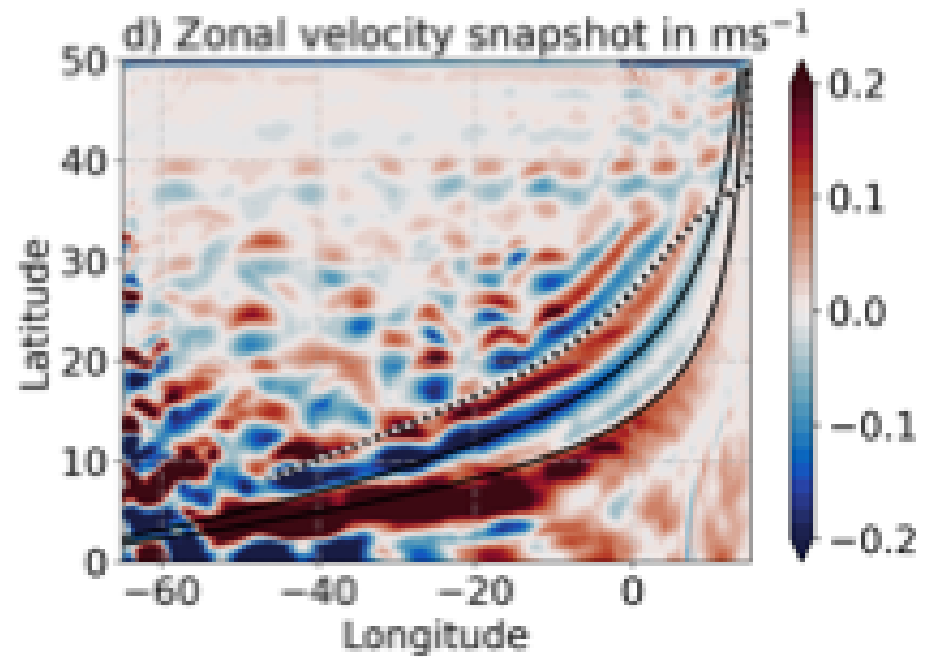
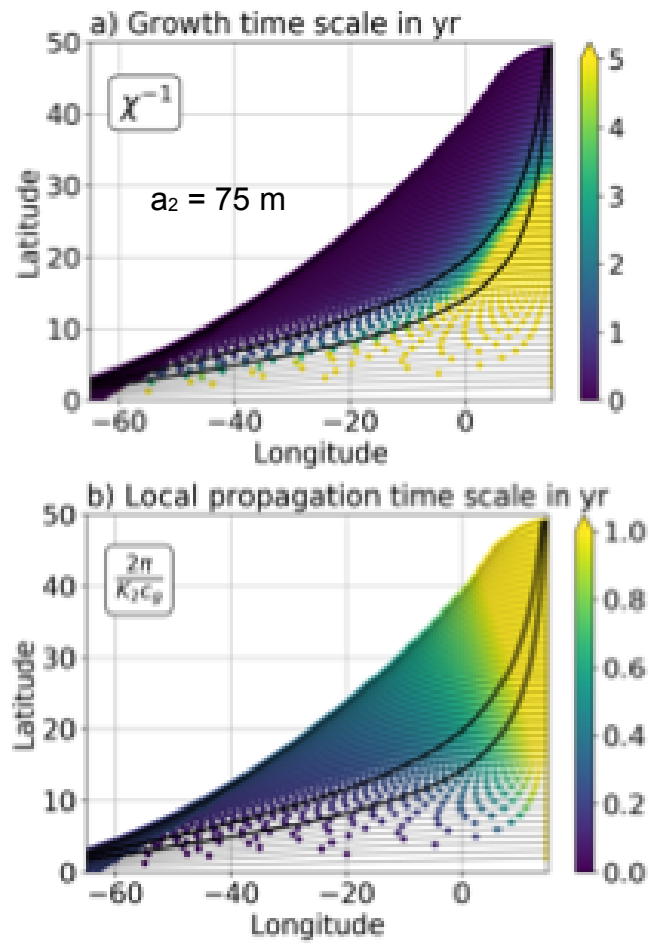
Variance



Variance

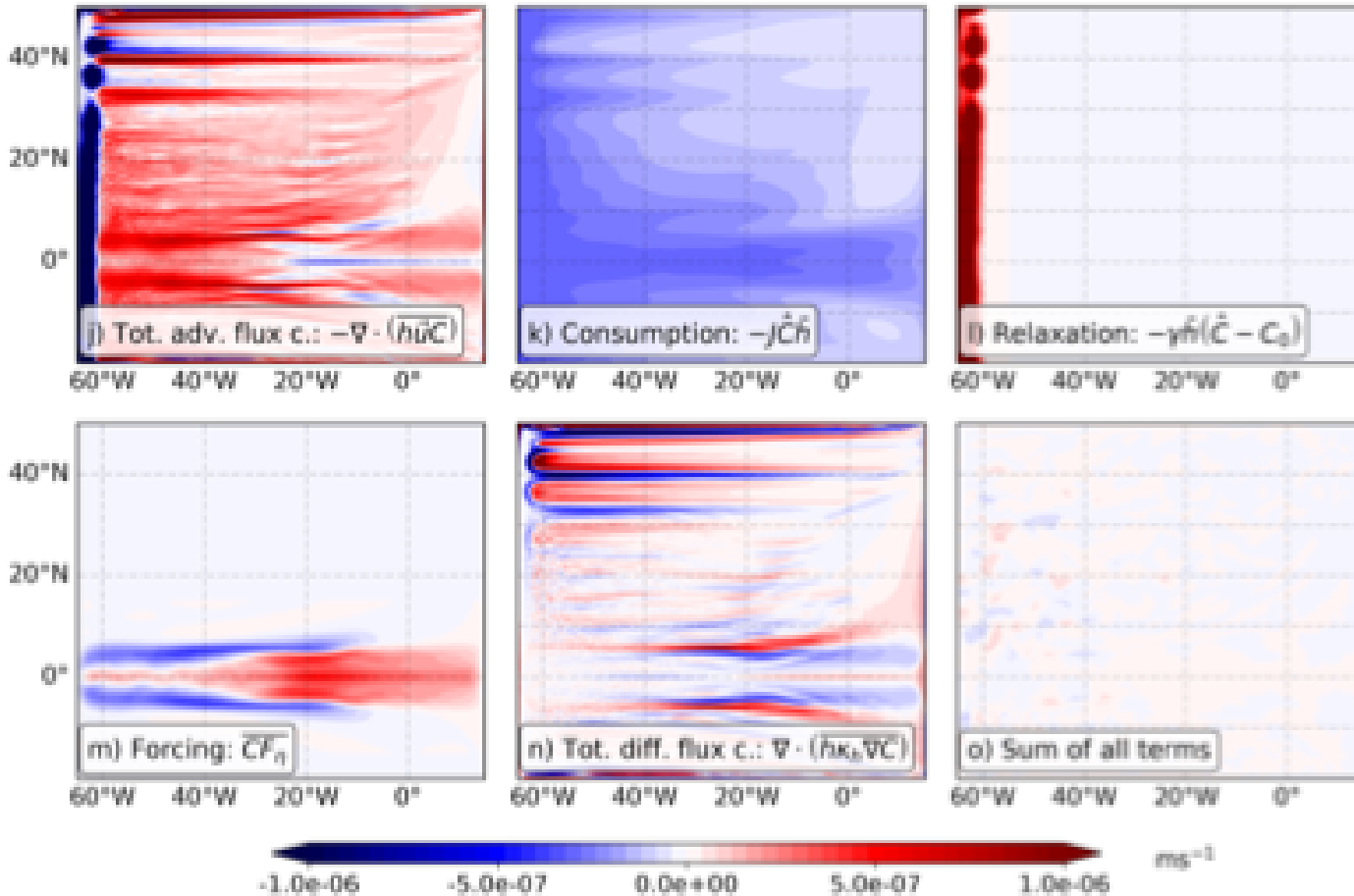


Zonal jet width - Non-linear triad instability

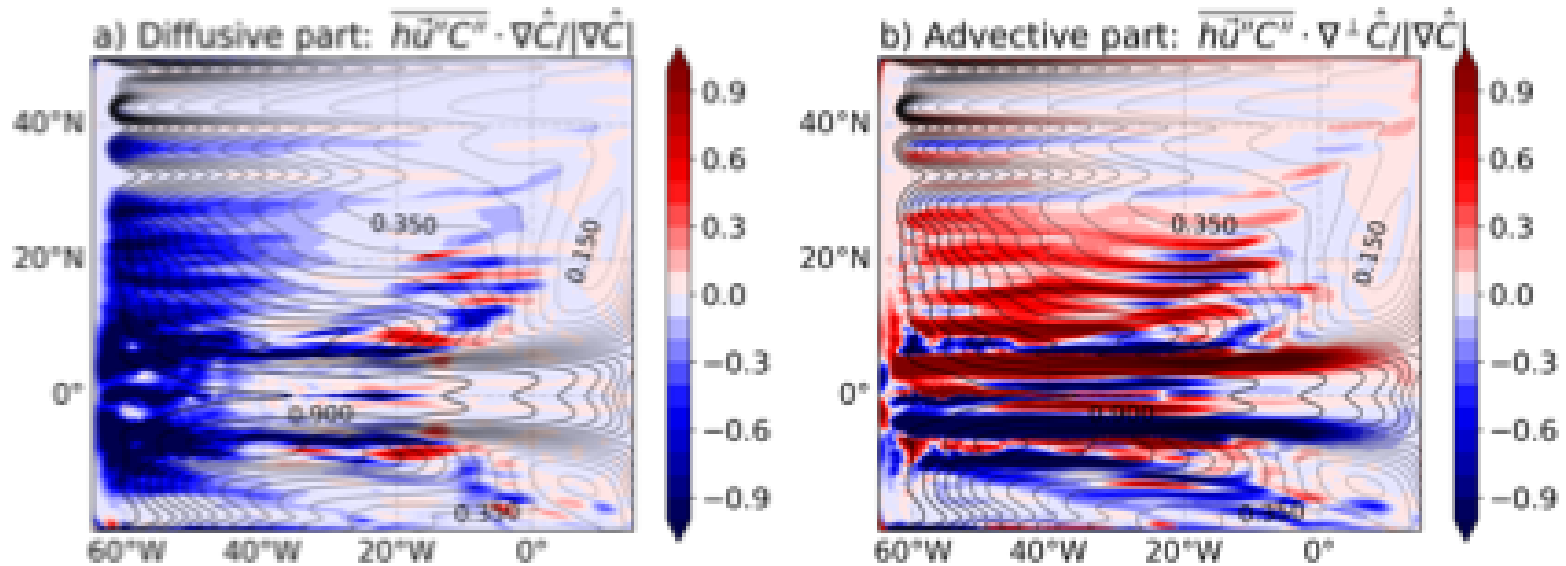


Projection onto the modelled field in spherical coordinates

Budget rectangle



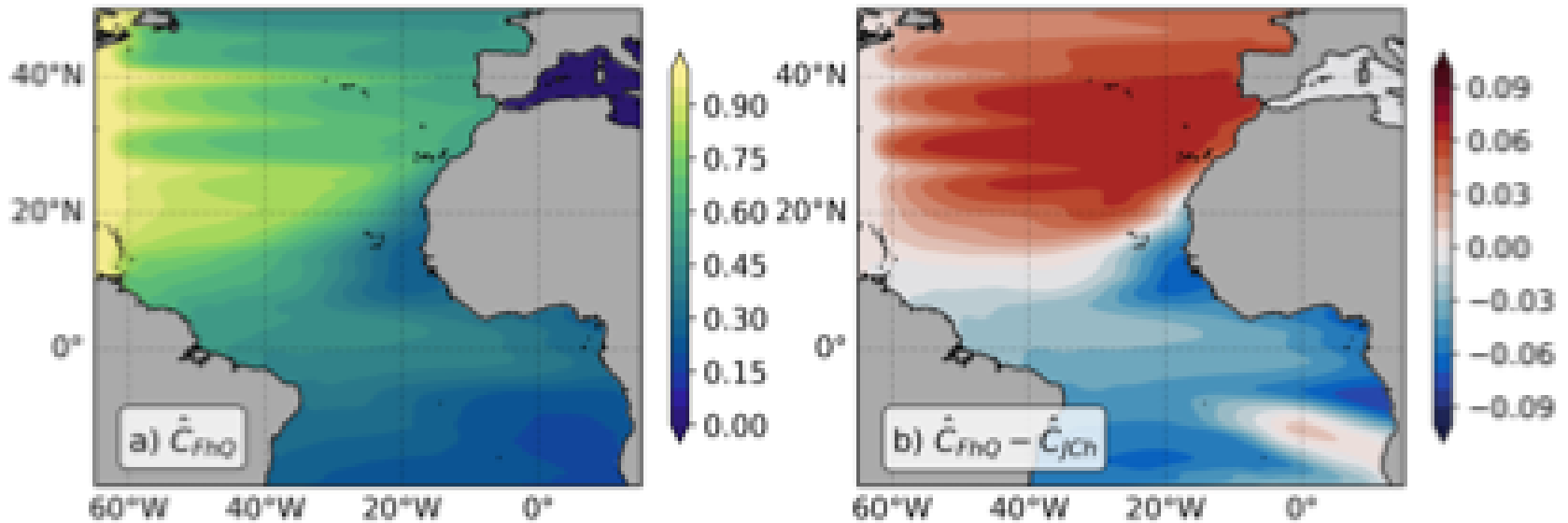
Eddy mixing rectangle



Different consumption scheme

consumption = $-FhQ$
 $F = 1$ if $C > 0.2$
 $F = 0$ else

as opposed to
 consumption = $-JCh$

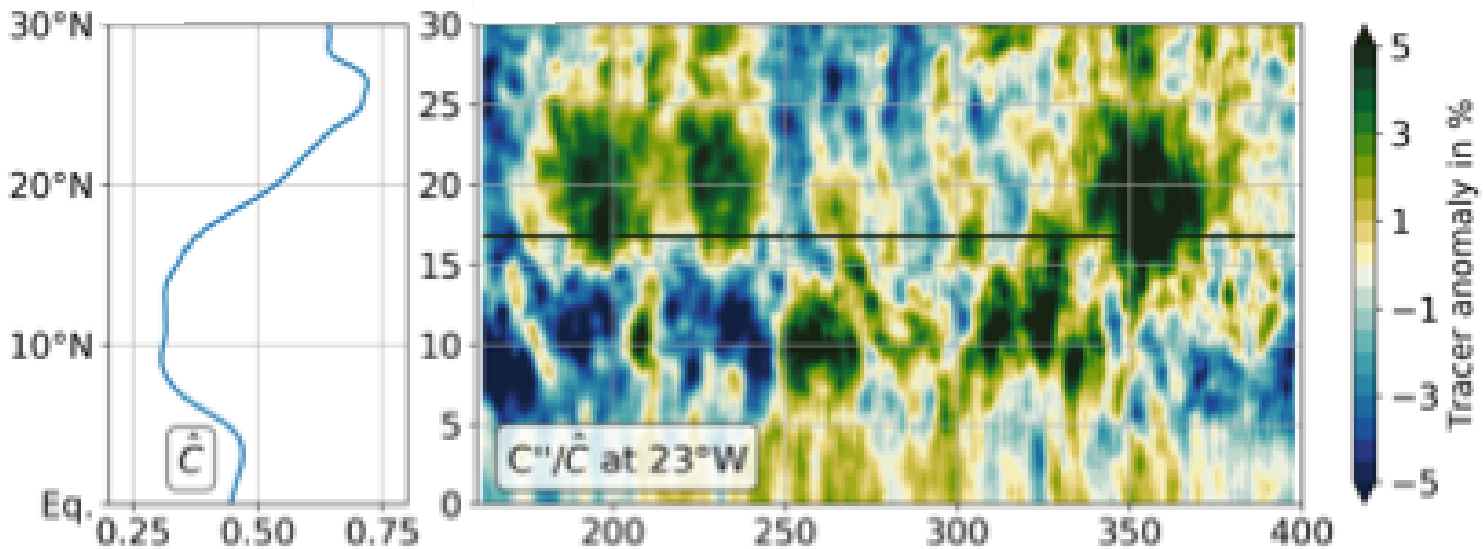


Different consumption scheme

$$\text{consumption} = -FhQ$$

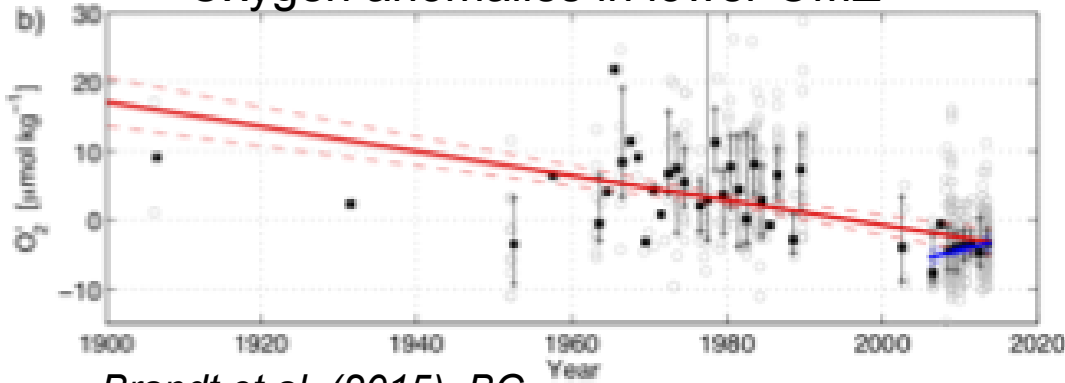
$$F = 1 \text{ if } C > 0.2$$

$$F = 0 \quad \text{else}$$



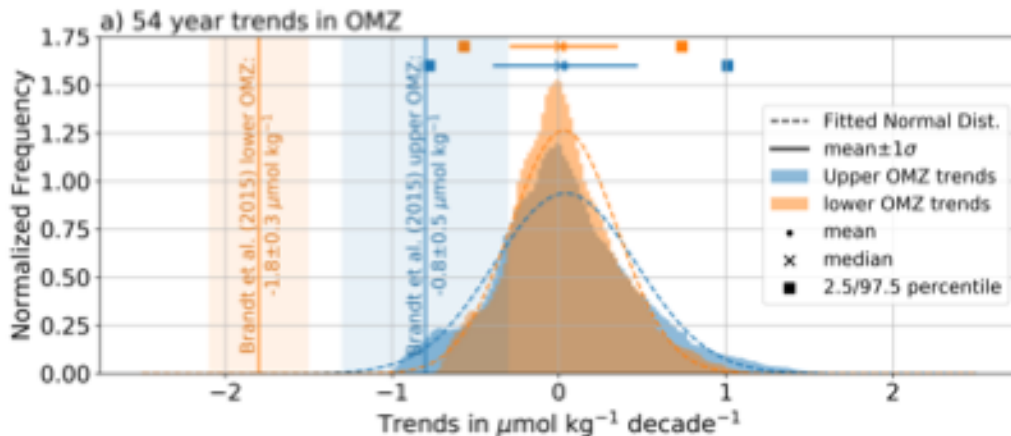
Compare trends for entire OMZ (9-15°N, 26-20°W)

Oxygen anomalies in lower OMZ



Brandt et al. (2015), BG

➡ facilitate a comparison scale modelled tracer concentrations to World Ocean Atlas concentrations



➡ observed multi-decadal trends in lower OMZ are not captured by modelled tracer field

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Merci beaucoup pour votre attention